

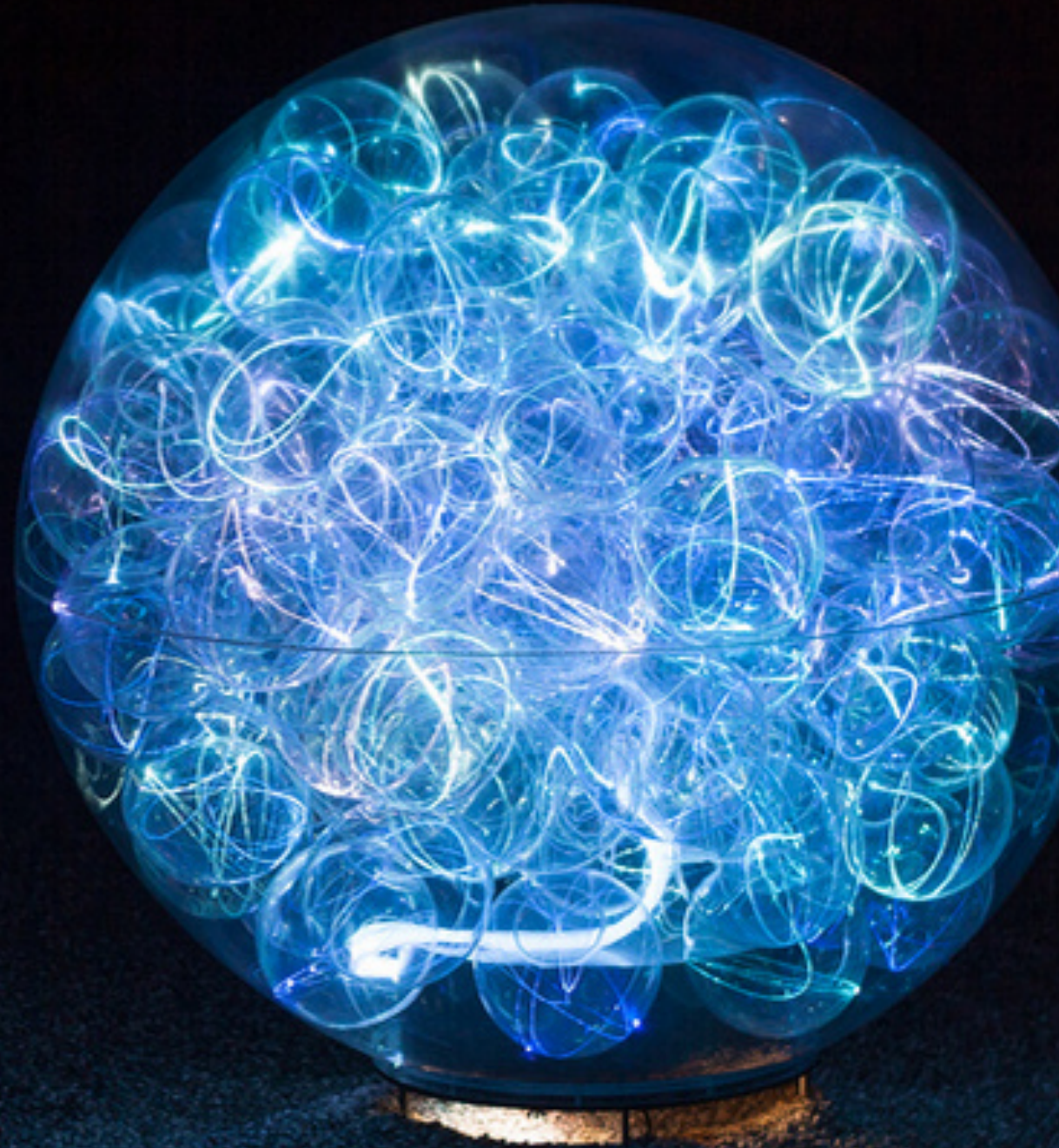
Silicon Photomultipliers:

Introducing the **digital** age in
low light detection



Rudjer Boskovic Institute
October 24th, 2018

Massimo Caccia
Dipartimento di Scienza & Alta Tecnologia
Uni. Insubria @Como, Italy
Massimo.caccia@uninsubria.it



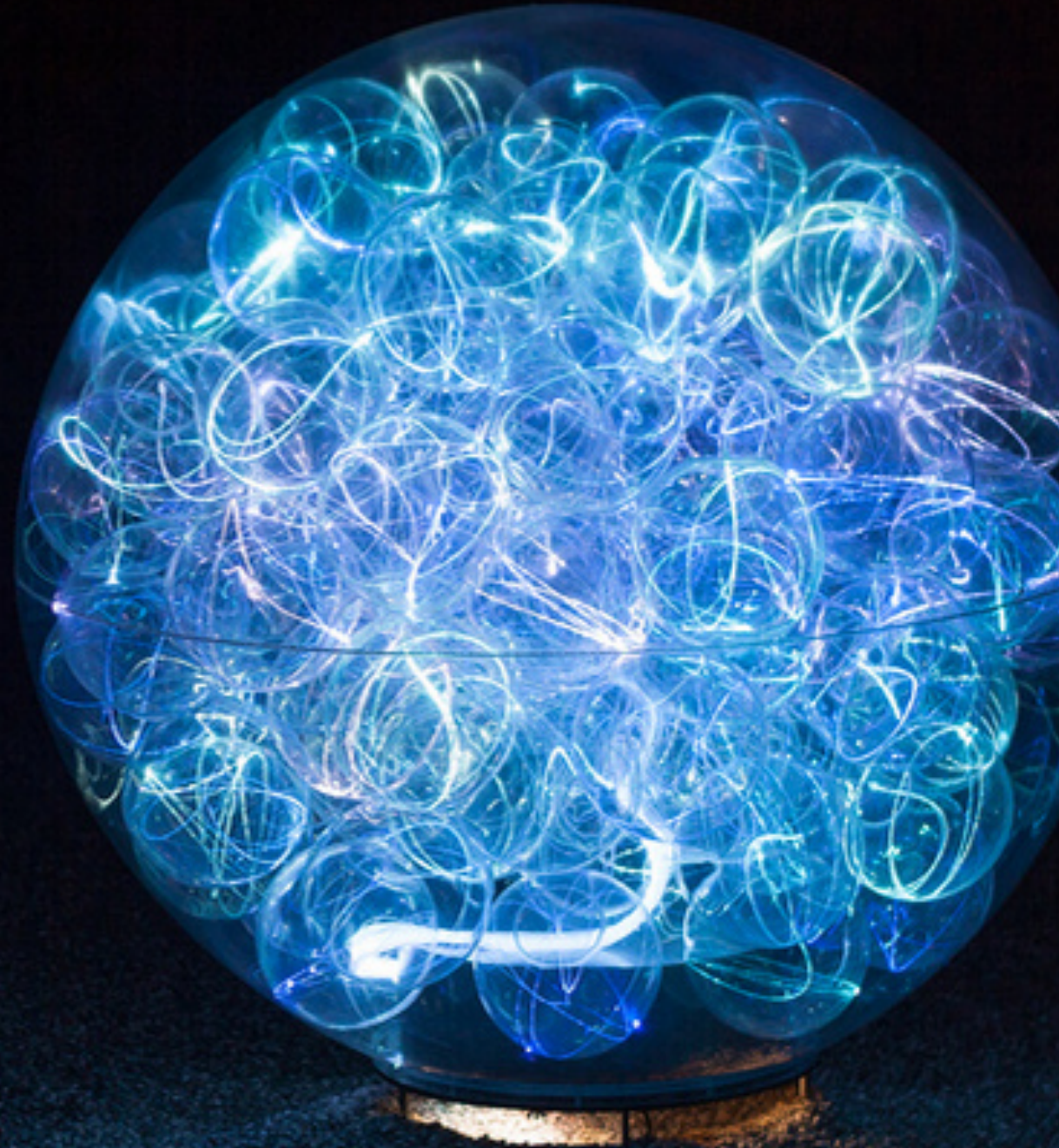
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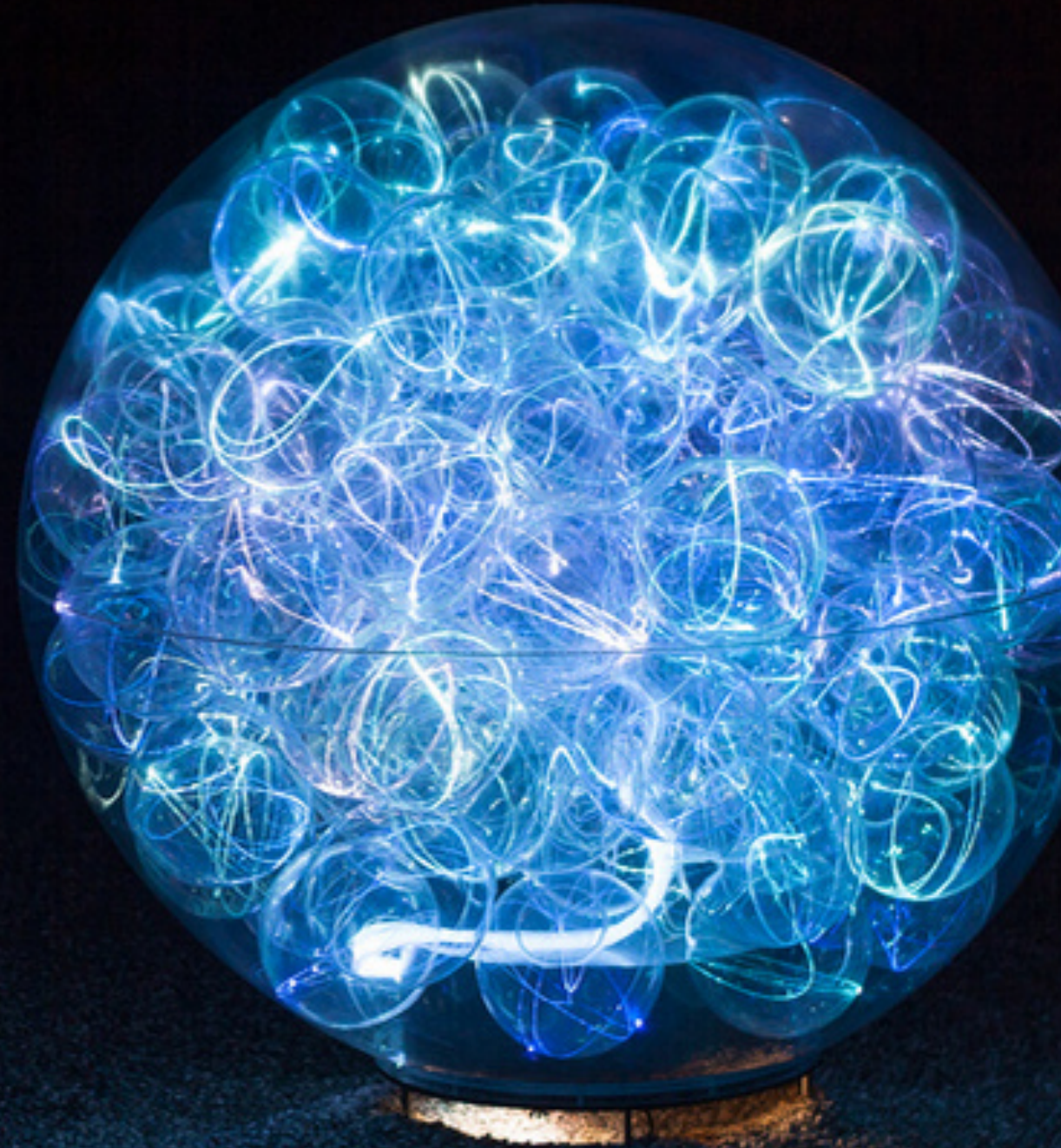


Silicon Photomultipliers:

Introducing the **Silicon** age in
low light detection

Part 1: principles, today & tomorrow

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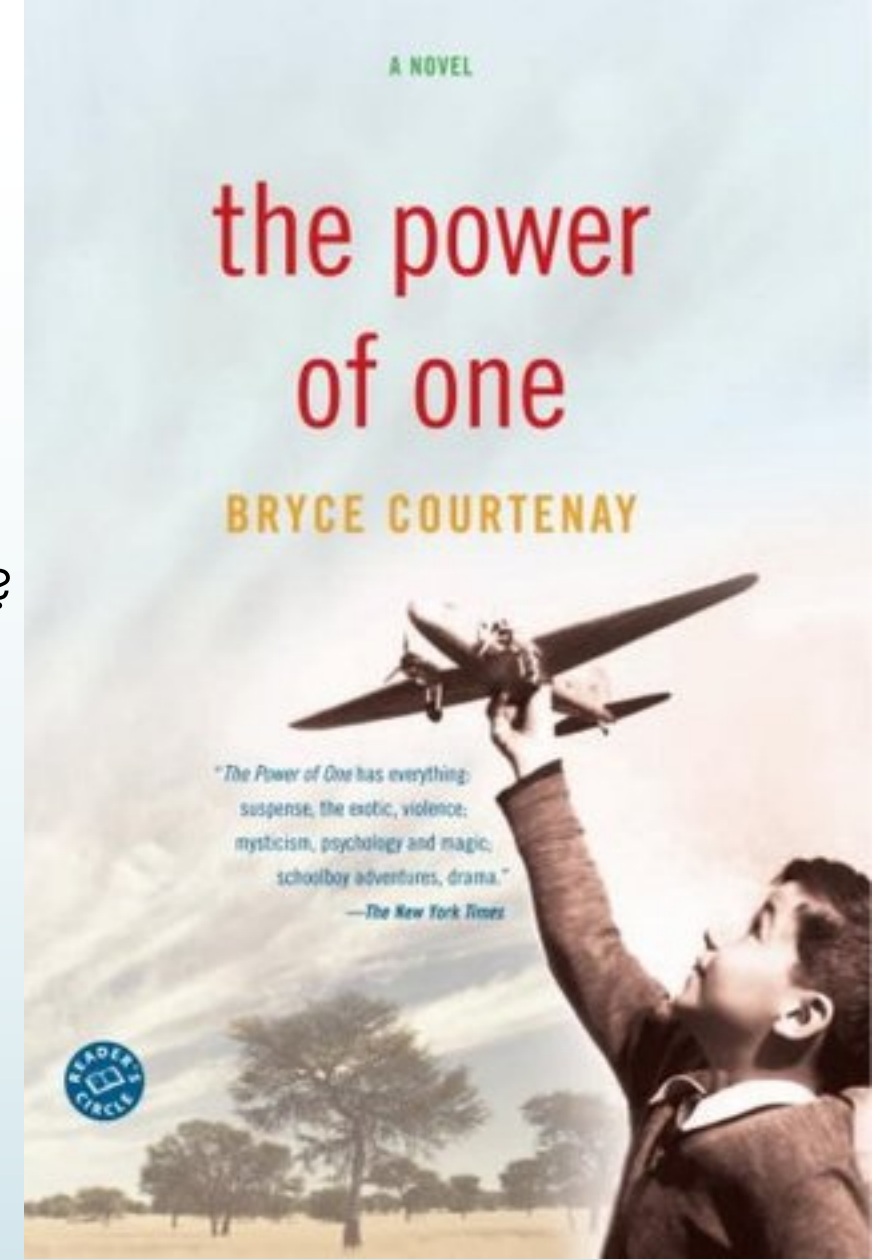




what if?

*

- I had a sensor with with single photon sensitivity?



* Credits: <https://what-if.xkcd.com>
Randall Munroe



The book: **What If?** Serious Scientific
Answers to Absurd Hypothetical Questions



what if?

- I had a sensor retaining at the same time the capability of measuring the intensity, possibly **counting the photons** in the light pulse illuminating the sensor (at the same time)?

Can I have a little more?*

1



2



4



3

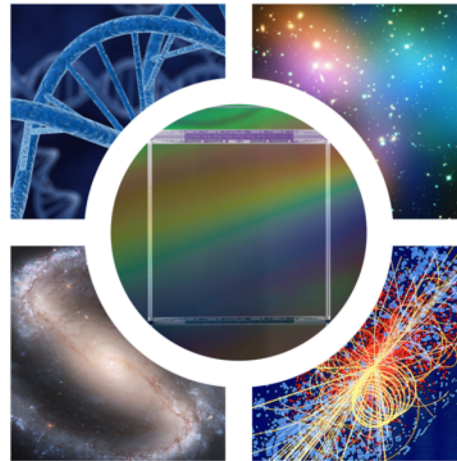




what if?

- I had a sensor with Position Sensitivity in 4D [namely telling me **where** & **when** the photon(s) hit the detector]?

PSD11



The Position Sensitive Detector
Conference
Milton Keynes, UK
September 2017

**The
Economist**

MARCH 11TH-17TH 2017

Ryancare attacked from left and right

IS up against the wall in Mosul

Taiwan and the one-China fiction

Is there a bubble in the markets?

Quantum leaps



A mind-bending technology goes mainstream

March 11th, 2017 Issue

I would probably be able to confirm what **valuable people** think (or presume to know):

[QuantumLeaps - March 2017](#)

And make them happy*



* It looks like an M&M, isn't it?

Well, maybe not all of them:



But I could anyway do a lot...

Engineering single photon (**deterministic!**) sources and **photon number resolving** sensors is actually the name of the game in “quantum” technologies [**cryptology**, computing, networks]

Eur. Phys. J. D (2012) 66: 249
DOI: 10.1140/epjd/e2012-30351-6

THE EUROPEAN
PHYSICAL JOURNAL D

Regular Article

Effect of the heralding detector properties on the conditional generation of single-photon states

V. D'Auria¹, O. Morin², C. Fabre², and J. Laurat^{2,a}

¹ Laboratoire de Physique de la Matière Condensée, CNRS UMR 7336, Université de Nice-Sophia Antipolis, Parc Valrose, 06108 Nice Cedex 2, France

² Laboratoire Kastler Brossel, Université Pierre et Marie Curie, École Normale Supérieure, CNRS, Case 74, 4 place Jussieu, 75252 Paris Cedex 05, France

Received 4 June 2012

Published online 4 October 2012 – © EDP Sciences, Società Italiana di Fisica, Springer-Verlag 2012

Abstract. Single-photons play an important role in emerging quantum technologies and information processing. An efficient generation technique consists in preparing such states via a conditional measurement on photon-number correlated beams: the detection of a single-photon on one of the beam can herald the generation of a single-photon state on the other one. Such scheme strongly depends on the heralding detector properties, such as its quantum efficiency, noise or photon-number resolution ability. These parameters affect the preparation rate and the fidelity of the generated state. After reviewing the theoretical description of optical detectors and conditional measurements, and how both are here connected, we evaluate the effects of these properties and compare two kinds of devices, a conventional on/off detector and a two-channel detector with photon-number resolution ability.

The characterization of the statistics of photons emitted by a classical and quantum source is essential. This is requiring sensors with PHOTON NUMBER RESOLVING CAPABILITY.

See also: M. Ramilli, M.C. et al, J. Opt. Soc. Am. B, Vol. 27, No. 5, May 2010



ARTICLE

Received 28 May 2013 | Accepted 10 Sep 2013 | Published 10 Oct 2013

DOI: 10.1038/ncomms3582

OPEN

Integrated spatial multiplexing of heralded single-photon sources

M.J. Collins¹, C. Xiong¹, I.H. Rey², T.D. Vo^{1,3}, J. He¹, S. Shahnian¹, C. Reardon⁴, T.F. Krauss^{2,4}, M.J. Steel⁵, A.S. Clark¹ & B.J. Eggleton¹

The non-deterministic nature of photon sources is a key limitation for single-photon quantum processors. Spatial multiplexing overcomes this by enhancing the heralded single-photon yield without enhancing the output noise. Here the intrinsic statistical limit of an individual source is surpassed by spatially multiplexing two monolithic silicon-based correlated photon pair sources in the telecommunications band, demonstrating a 62.4% increase in the heralded single-photon output without an increase in unwanted multipair generation. We further demonstrate the scalability of this scheme by multiplexing photons generated in two waveguides pumped via an integrated coupler with a 63.1% increase in the heralded photon rate. This demonstration paves the way for a scalable architecture for multiplexing many photon sources in a compact integrated platform and achieving efficient two-photon interference, required at the core of optical quantum computing and quantum communication protocols.



KUNGL.
VETENSKAPS-
AKADEMIEN

THE ROYAL SWEDISH ACADEMY OF SCIENCES

8 OCTOBER 2014



Scientific Background on the Nobel Prize in Chemistry 2014

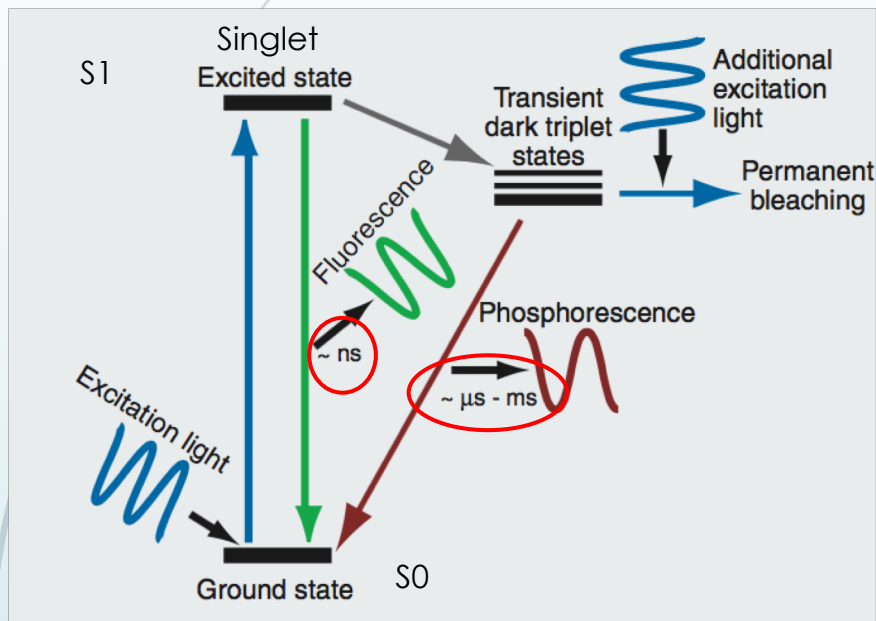
SUPER-RESOLVED FLUORESCENCE MICROSCOPY

Awarded to: Eric Betzig, Stefan W. Hell, William E. Moerner

Method of the Year 2008

With its tremendous potential for understanding cellular biology now poised to become a reality, super-resolution fluorescence microscopy is our choice for Method of the Year.

Heralded by Nature:



States and transitions of a fluorophore

Key issues:

- The lifetime of the emission from the Triplet state is $O(10^6)$ wrt Singlet
- The transition probability to the Triplet state is $O(0.1\%)$

⇒ with a continuous excitation of intensity 1 kW/cm^2 the fraction of molecules in $S_0 \ll 10\%$

and for every cycle you will see a subset of molecules *blinking*

- [Sub-diffraction limit imaging by stochastic optical reconstruction microscopy \(STORM\)](#)

Rust et al., Nature Methods vol.3 NO.10 | OCTOBER 2006 | **793**

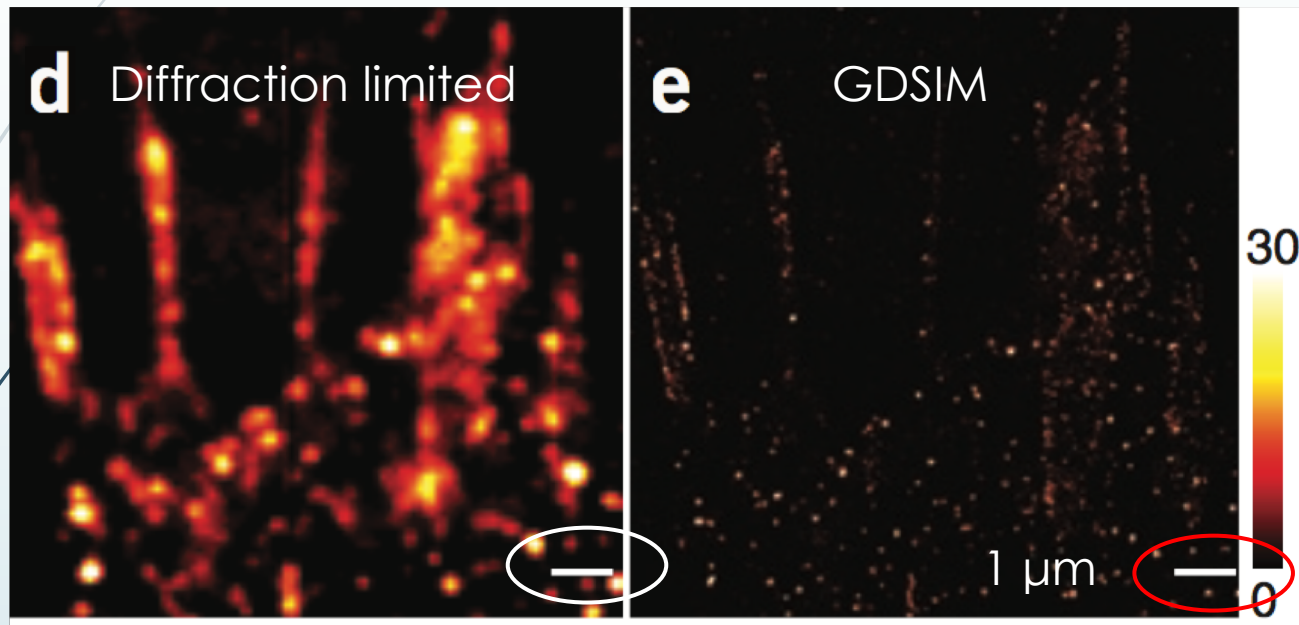
- [Fluorescence Nanoscopy by ground state depletion and single molecule return \(GDSIM\)](#)

Folling et al., Nature Methods vol.5 NO.11 | OCTOBER 2008 | 943

Method of the Year 2008

Heralded by Nature:

With its tremendous potential for understanding cellular biology now poised to become a reality, super-resolution fluorescence microscopy is our choice for Method of the Year.



- Camera frame: 200 Hz
- No. frames: 31 000
- Laser intensity: 2.5 kW/cm²
- Laser wavelength: 532 nm

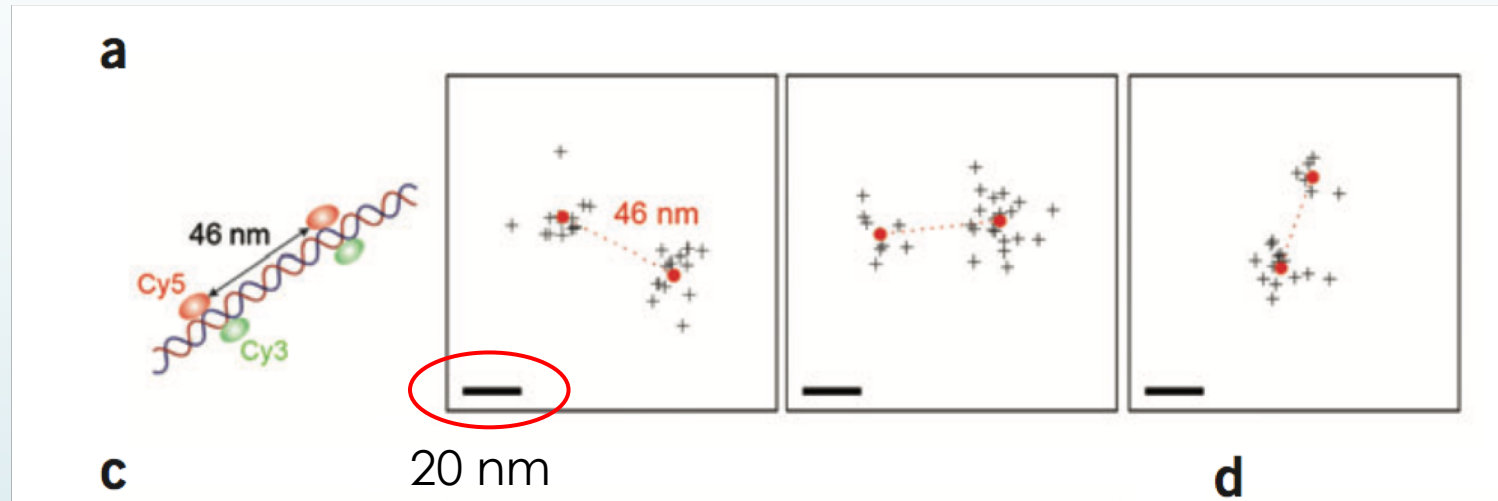
Immunostained (Atto532) integrin- β -3 clusters of human glioma cells in a cell medium

- [Fluorescence Nanoscopy by ground state depletion and single molecule return \(GDSIM\)](#)
Fölling et al., Nature Methods vol.5 NO.11 | OCTOBER 2008 | 943

Method of the Year 2008

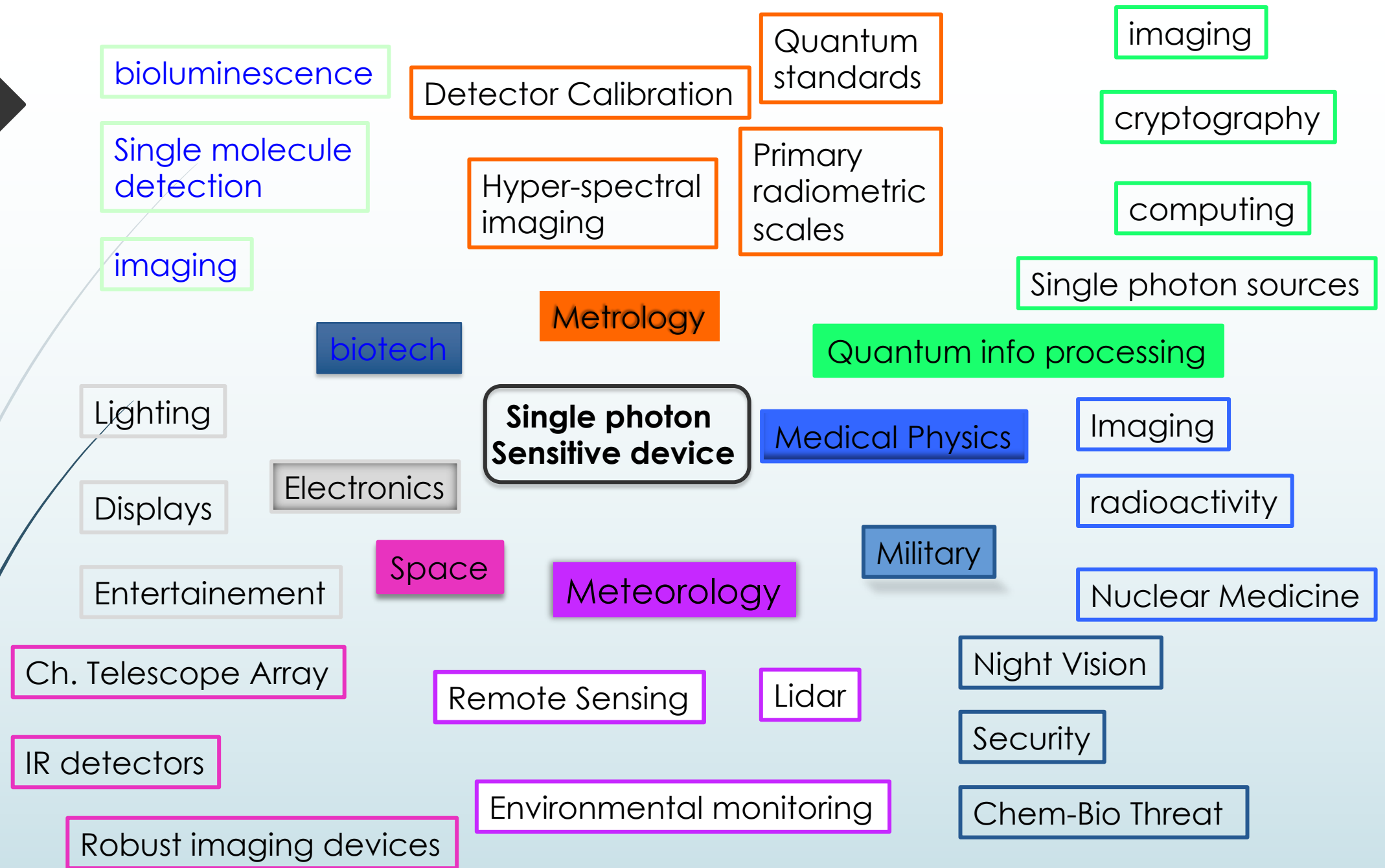
Heralded by Nature:

With its tremendous potential for understanding cellular biology now poised to become a reality, super-resolution fluorescence microscopy is our choice for Method of the Year.



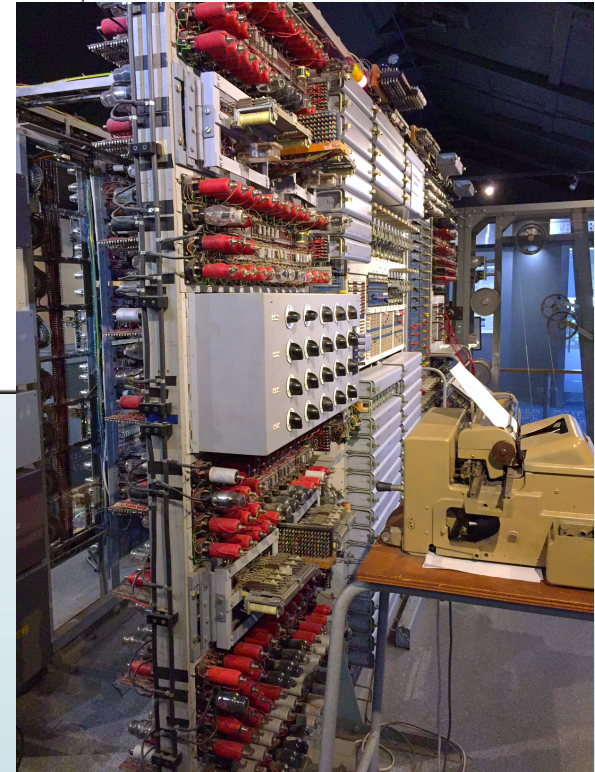
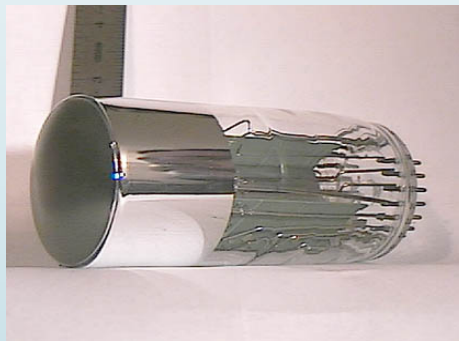
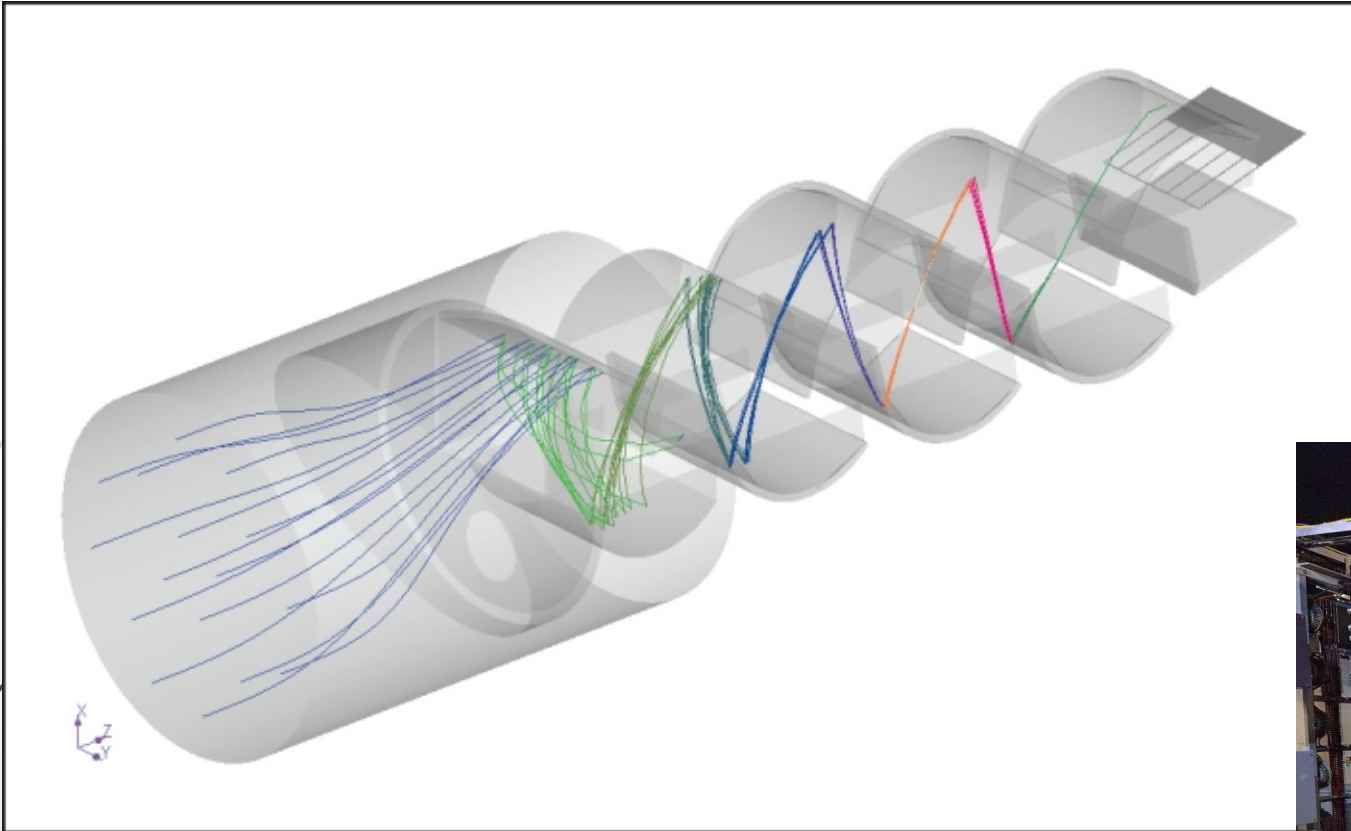
Separation between “switches” attached to a DNA molecule separated by a well known number of base pairs

- [Sub-diffraction limit imaging by stochastic optical reconstruction microscopy \(STORM\)](#)
Rust et al., Nature Methods vol.3 NO.10 | OCTOBER 2006 | 793



The pre-Silicon age:

the **photomultiplier**, a solid rock technology since 1934

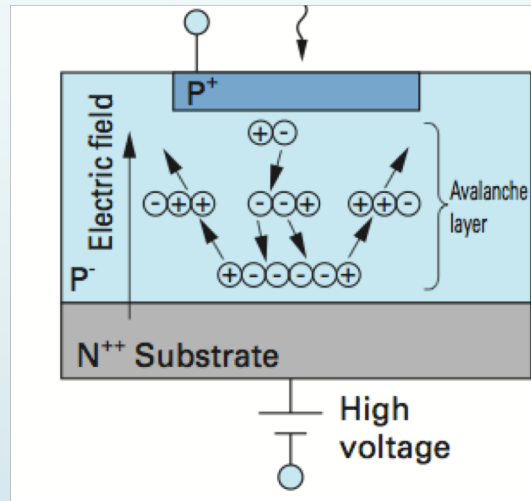


The Colossus (1944), containing on 1700 thermoionic valves

Photon absorption and avalanche ignition in a Single Photon Avalanche Photodiode (SPAD)

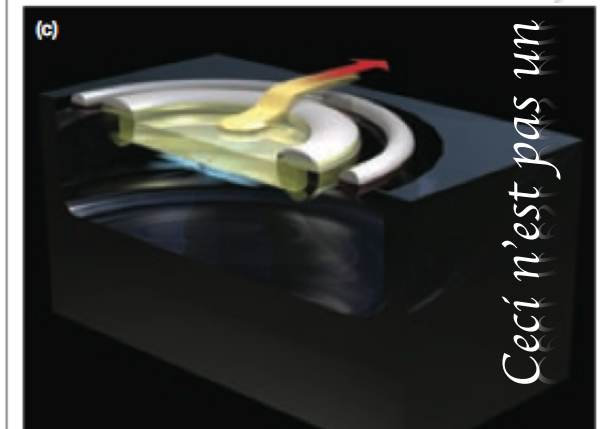
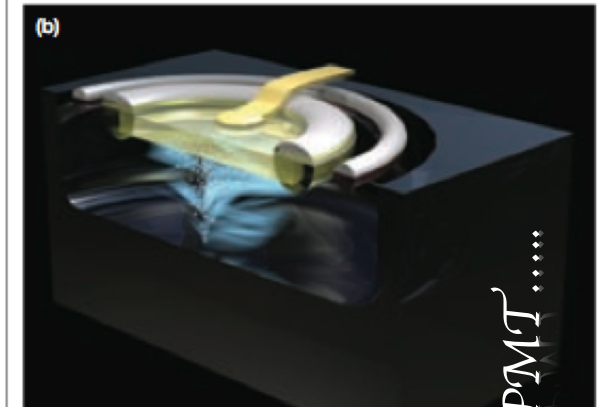
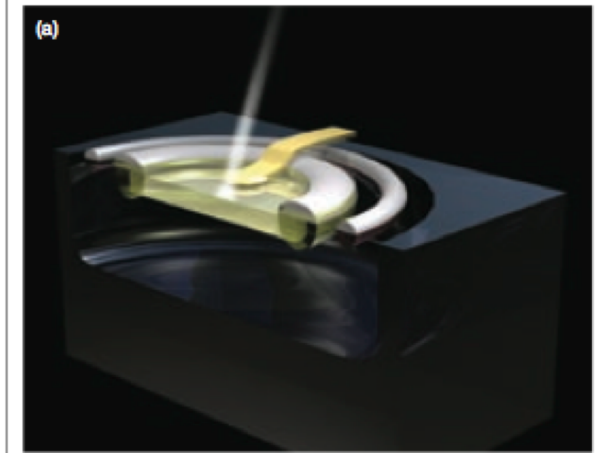
A pioneering development by Prof. S. Cova at Politecnico di Milano

Cova, S., Ghioni, M., Lacaita, A. L., Samori, C., and Zappa, F. "Avalanche photodiodes and quenching circuits for single-photon detection", Applied Optics, 35(12), 1956—1976 (1996)



- Very shallow p-n junction
→ $\sim 1 \mu\text{m}$
- High electric field
→ $> 3 \times 10^5 \text{ V/cm}$
- Mean free path
 $\approx 0.01 \mu\text{m}$

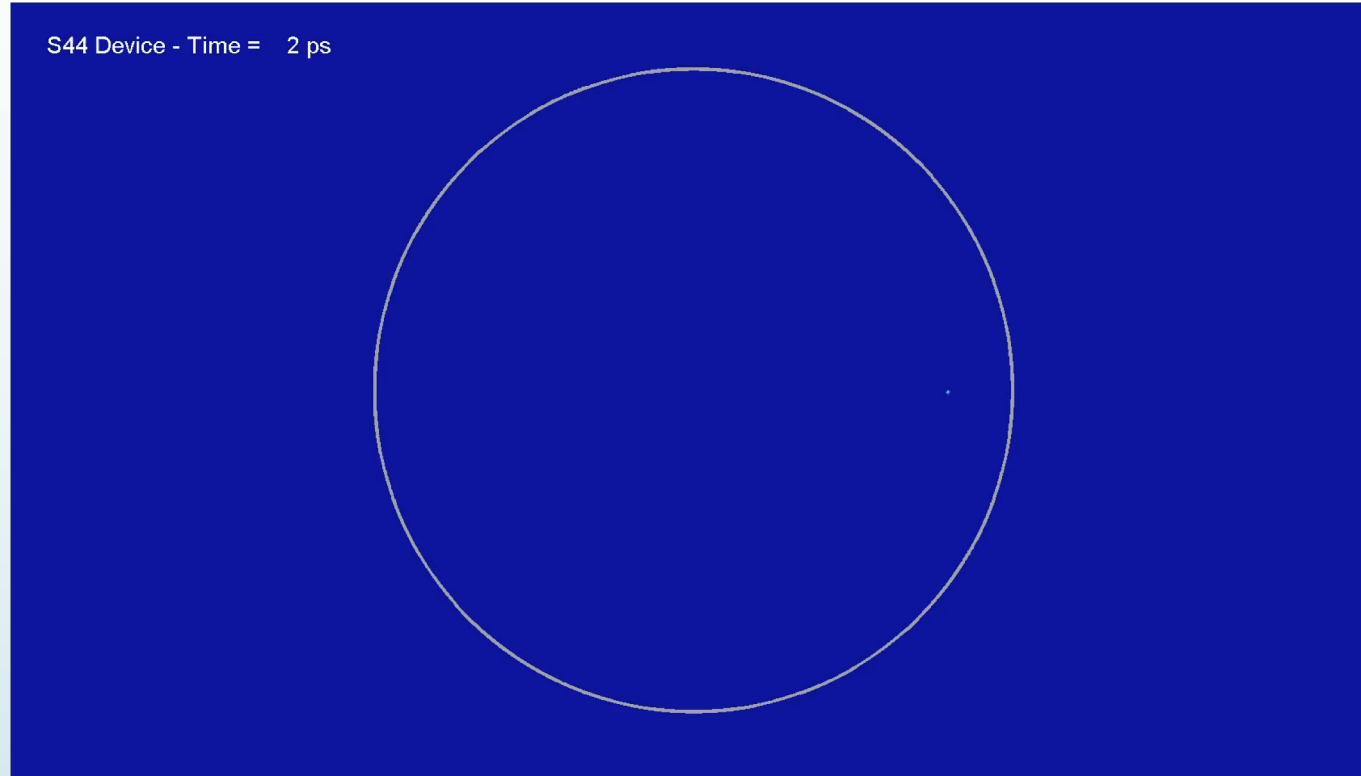
... and when you get to an array, a matrix of SPAD, you get to the main subject of this talk



Ceci n'est pas un PMT....

A multiplication game in Silico

Courtesy Ivan Rech, Politecnico di Milano

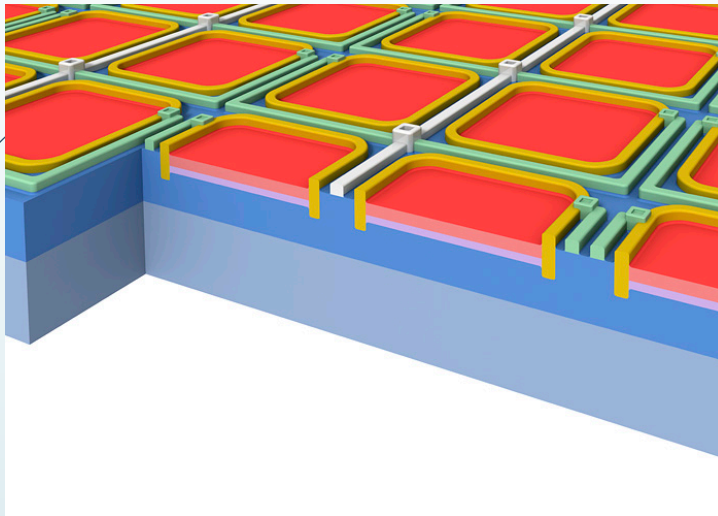


- ❖ Spread of the avalanche essentially diffusion assisted (with minor contributions from photons)
- ❖ Speed 10-20 $\mu\text{m}/\text{ns}$ (this cell has a diameter of 50 μm)

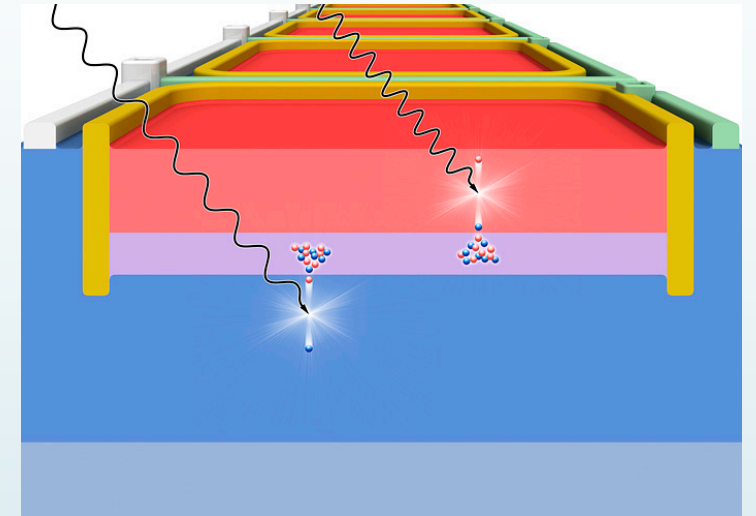
1. **A. Gulinatti, I. Rech, M. Assanelli, M. Ghioni & S. Cova** (2011) A physically based model for evaluating the photon detection efficiency and the temporal response of SPAD detectors, *Journal of Modern Optics*, 58:3-4, 210-224, DOI: 10.1080/09500340.2010.536590
2. **A. Gulinatti, I. Rech et al.**, Modeling photon detection efficiency and temporal response of single photon avalanche diodes, *Proc. of SPIE Vol. 7355 73550X-1*
3. **Spinelli, A. and Lacaita, A. L.** "Physics and numerical simulation of single photon avalanche diodes", *IEEE Transactions on Electron Devices*, 44(11), 1931—1943 (1997).

Silicon PhotoMultipliers (a.k.a. as MPPC, for MultiPixel Photon Counters): in essence, an array of SPADs

Principle



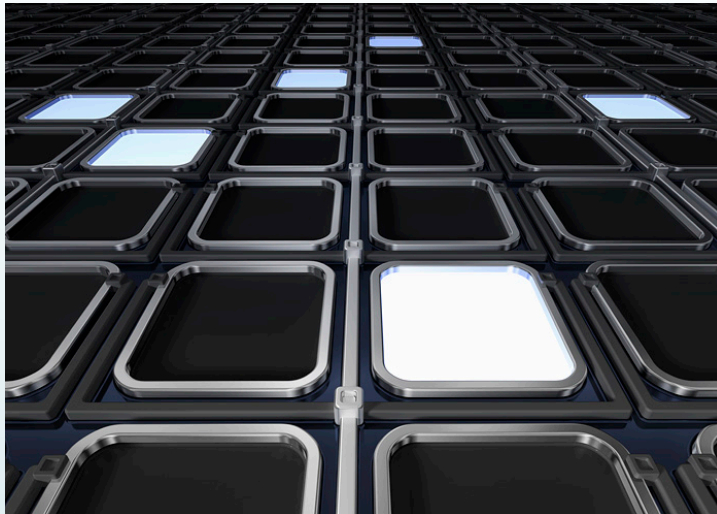
SiPM = High density ($\sim 10^4/\text{mm}^2$) matrix of diodes with a common output, reverse biased, working in Geiger-Müller regime



When a photon hits a cell, the generated charge carrier triggers an avalanche multiplication in the junction by impact ionization, with gain at the 10^6 level

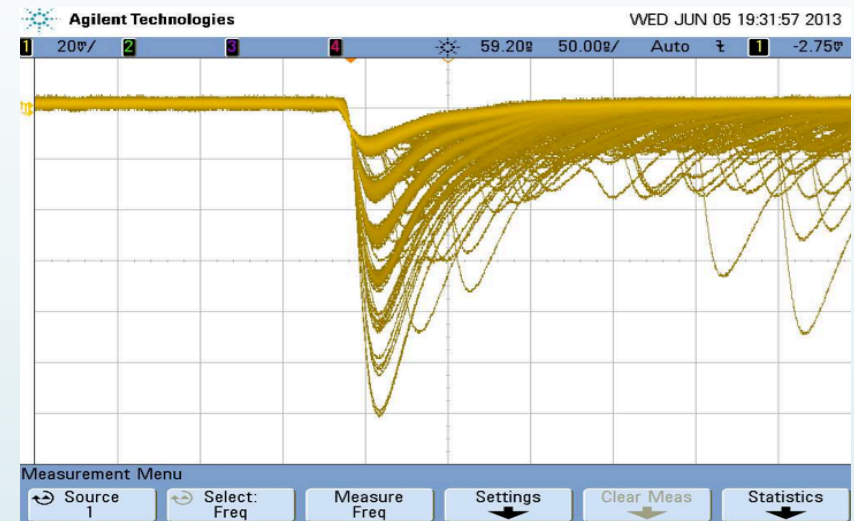
Silicon Photomultipliers: genuine digital Photon Number Resolving detectors

Operation



- SiPM may be seen as a collection of binary cells, fired when a photon is absorbed

[in principle, a NATIVE DIGITAL DEVICE]



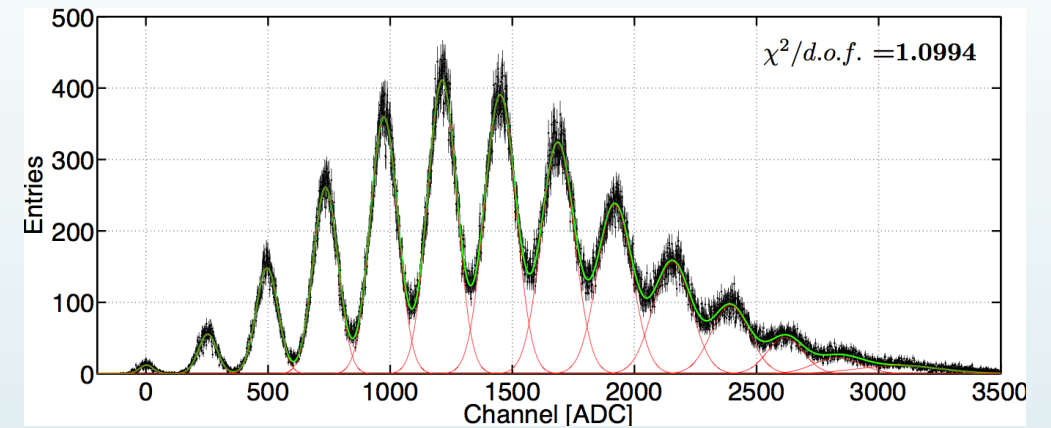
- “counting” cells provides an information about the intensity of the incoming light:

Silicon Photomultipliers: genuine digital Photon Number Resolving detectors

Operation



- SiPM may be seen as a collection of binary cells, fired when a photon is absorbed



- “counting” cells provides an information about the intensity of the incoming light:

There's a lot of



behind the SiPM concept
and technology



With reference to the paper:
A. Gasanov, V. Golovin, Z. Sadigov, N. Yusipov, Avalanche
photodetector on base metal-resistor-semiconductor structure,
Microelectronics, 1989



ELSEVIER

Nuclear Instruments and Methods in Physics Research A 442 (2000) 223–229

NUCLEAR
INSTRUMENTS
& METHODS
IN PHYSICS
RESEARCH
Section A

www.elsevier.nl/locate/nima

Silicon avalanche photodiodes on the base of metal-resistor-semiconductor (MRS) structures

V. Saveliev^{a,*}, V. Golovin^b

^aMoscow Engineering and Physics Institute, Kashirskoe Shosse 31, 115409 Moscow, Russia

^bCenter of Perspective Technology and Apparatus, Moscow, Russia



ELSEVIER

Nuclear Physics B (Proc. Suppl.) 61B (1998) 347–352

NUCLEAR PHYSICS B
PROCEEDINGS
SUPPLEMENTS

Limited Geiger-mode silicon photodiode with very high gain

G. Bondarenko^a, B. Dolgoshein^a, V. Golovin^b, A. Ilyin^a, R. Klanner^c, E. Popova^a

^aMoscow Engineering and Physics Institute (MEPHI), Russia

^bCentre of Perspective Technology and Apparatus (CPTA), Moscow, Russia

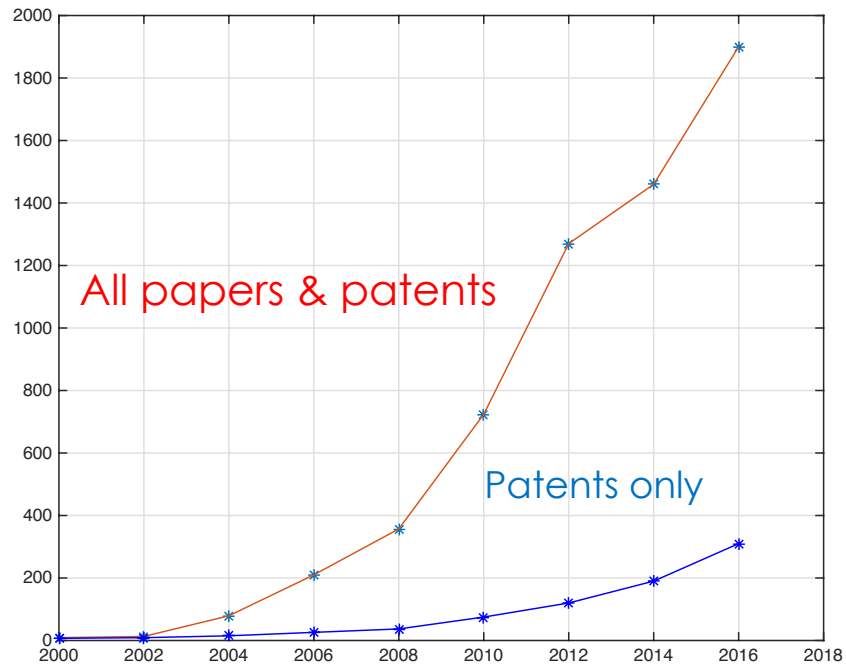
^cDESY, Hamburg, Germany

The novel type of the Silicon Photodiode – Limited Geiger-mode Photodiode (LGP) has been produced and studied. The device consists of many $\approx 10^4$ mm⁻² independent cells ≈ 10 mkm size around n⁺-“pins” located between p-substrate and thin SiC layer. Very high gain more than 10^4 for 0.67 mkm wave length light source and up to $6 \cdot 10^5$ for single electron have been achieved. The LGP photon detection efficiency at the level of one percent has been measured.

With a series of early patents also
assigned to Russian inventors

Is the world interested in these little toys?

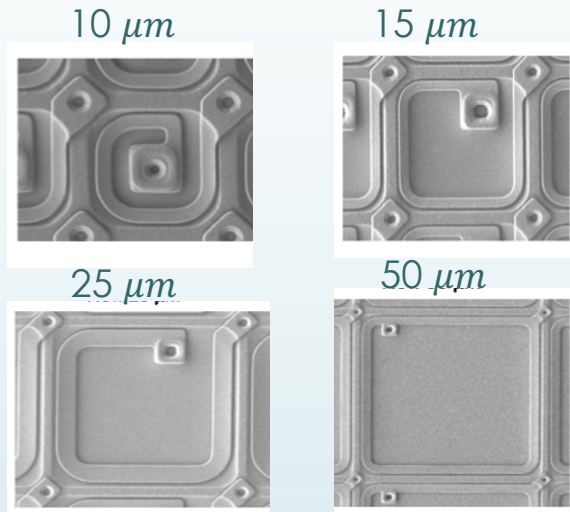
No. of papers in [Google Scholar](#) with the exact match of “silicon photomultiplier^s” in the title/abstract/body



Year	# papers	Excluding patents
2000-2001	9	2
2002-2003	13	4
2004-2005	79	64
2006-2007	210	184
2008-2009	357	320
2010-2011	724	649
2012-2013	1270	1150
2014-2015	1460	1270
2016-2017	1900	1590

What is being offered on the “Menù à la carte?”

➤ In terms of pixel pitch:

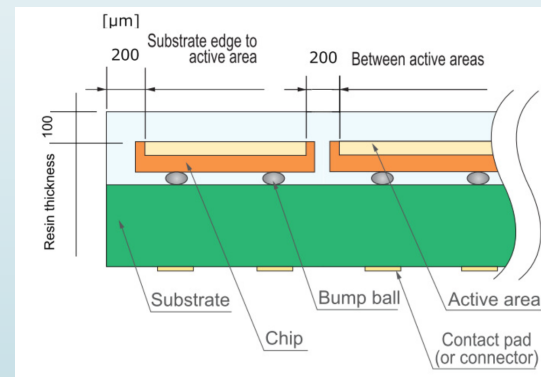
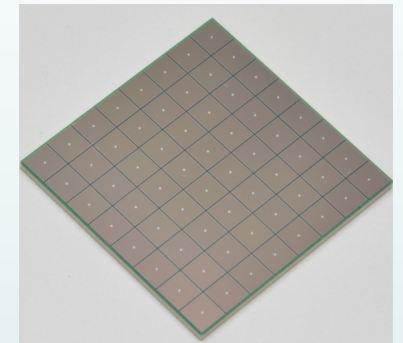


75 & 100 μm are available as well

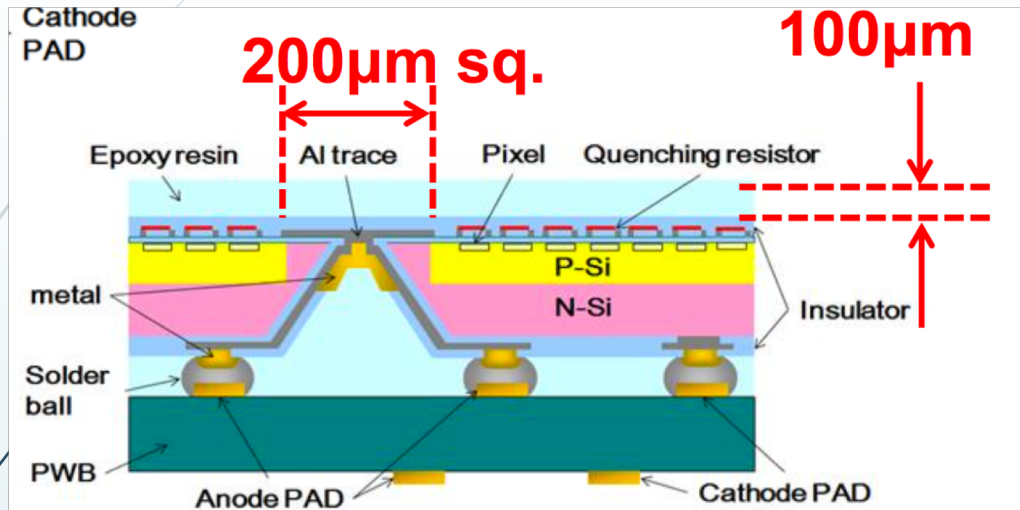
Not to mention the variety of available options for the front-end, the **packaging** and the near future integration with the read-out electronics

➤ In terms of sensor area:

- 1x1 mm²
- 3x3 mm²
- 6x6 mm²
-
- 1x4 mm²
- 12x12 mm²
- 24x24 mm²

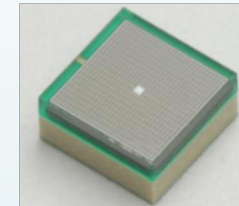


Talking about packaging, it is worth focusing on the “little white dot” in the middle of the array:

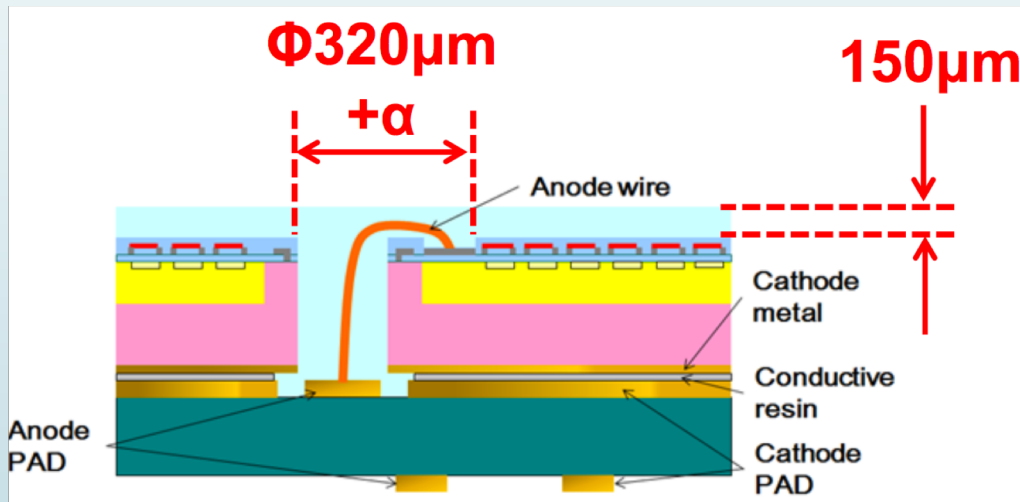


Through-Silicon Vias

- Makoto Motoyoshi, Proceedings of the IEEE, DOI: [10.1109/JPROC.2008.2007462](https://doi.org/10.1109/JPROC.2008.2007462), 2009
- Gambino et al., Microelectronic Engineering 135 (2015) 73–106



S13360 series



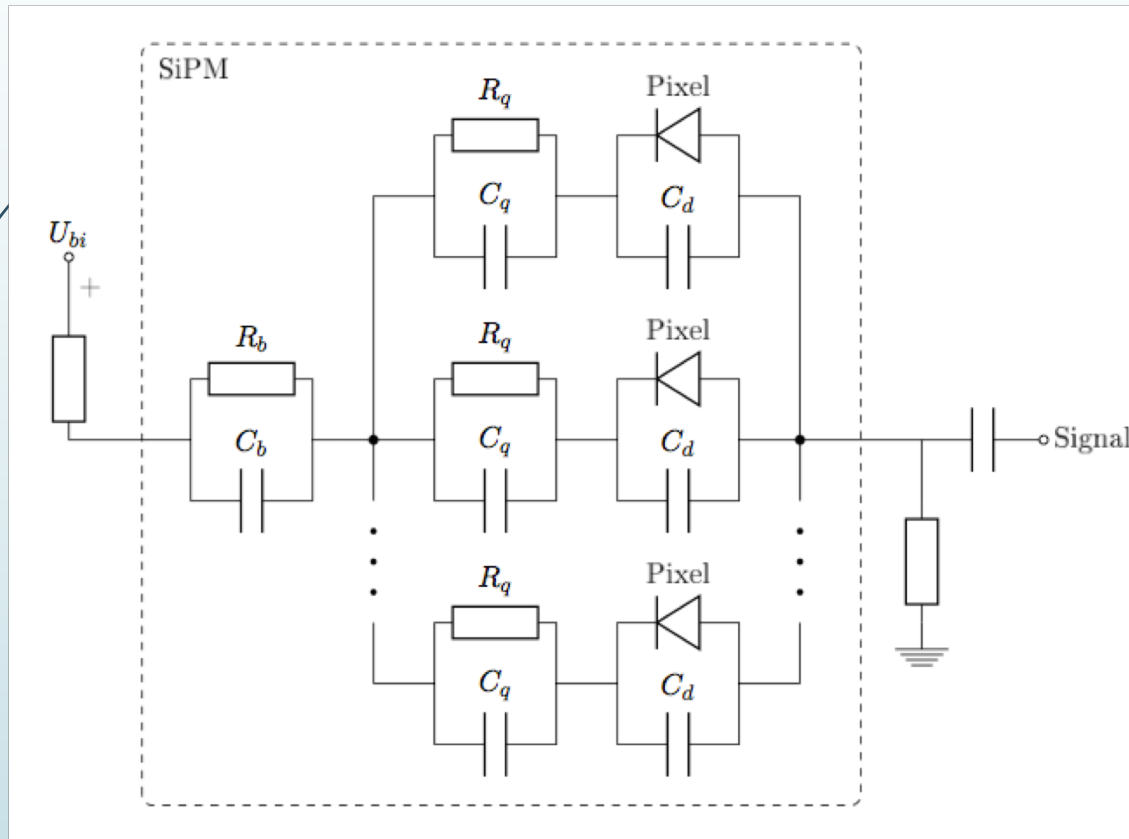
Hole-Wire bonding (patent pending)

S1416X series (X = 0,1)

LOWER COST, comparable specs

SiPM: electrical model(s)

1. Roland Heitz, *Journal of Applied Physics* **35**, 1370 (1964)
2. C. Piemonte, *NIM A* 568 (2006) 224–232
3. S. Seifert et al., *IEEE TRANSACTIONS ON NUCLEAR SCIENCE*, VOL. 57, NO. 4, 2010
4. P. Hallen, bachelor thesis, Aachen University, 2011
5. F.Licciulli, C.Marzocca, *IEEE TRANSACTIONS ON NUCLEAR SCIENCE*, VOL. 63, NO. 5, 2016
6. D. Marano et al., *Improved SPICE electrical model of SiPM*, *NIM A* 726, 1-7, 2013
7. F. Villa et al., *Spice electrical models and simulations of Silicon Photomultipliers*, *IEEE-TNS* October 2015



❖ exponential pulse with

$$\tau = R_q C_D$$

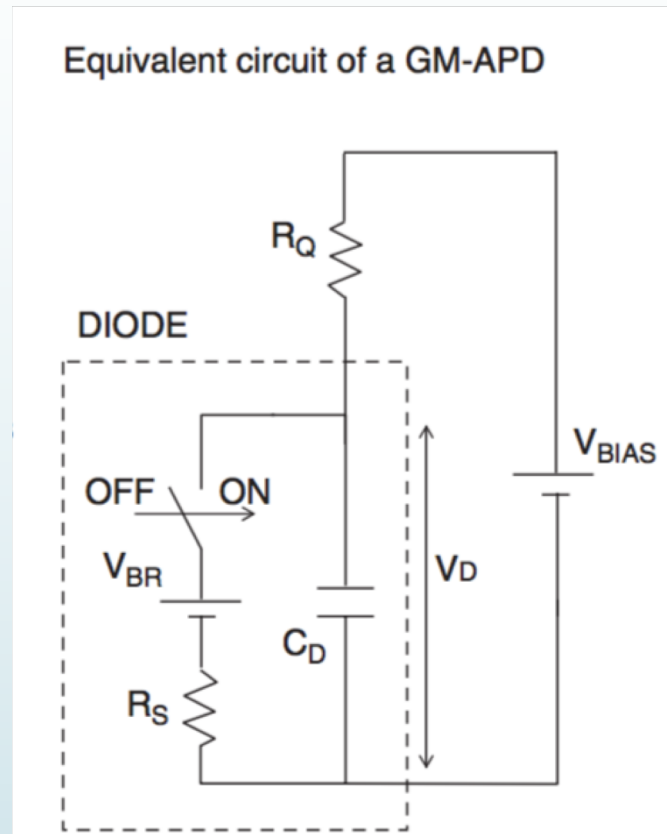
❖ Gain:

$$G = \frac{(V_{bias} - V_{Breakdown}) C_D}{e}$$

Typical values:

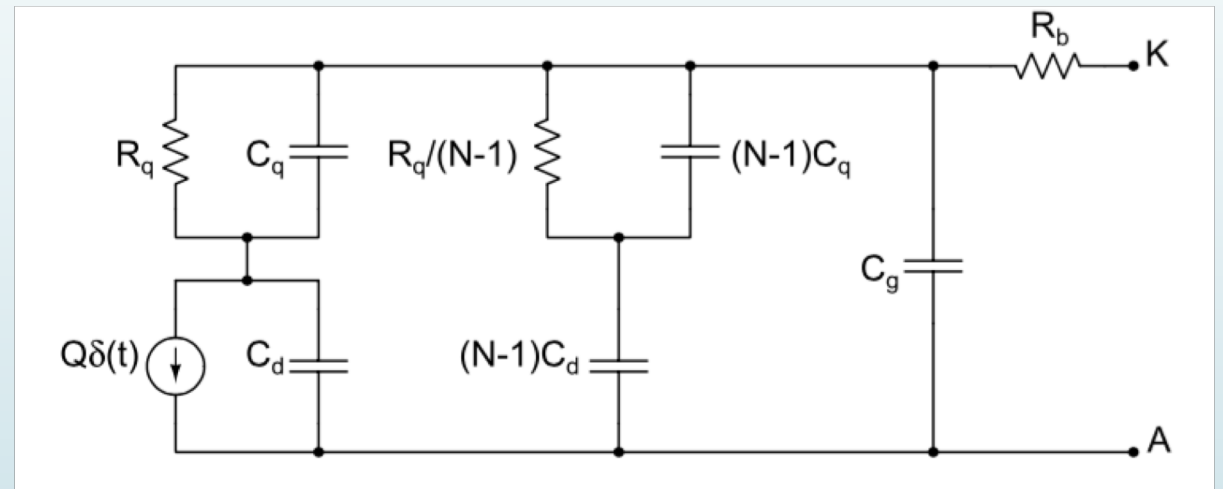
- ❖ $R_q \sim 200 \text{ k}\Omega$
- ❖ $C_D \sim 100 \text{ fF}$ ($30 \times 30 \text{ }\mu\text{m}^2$)
- ❖ $\tau \sim 20 \text{ ns}$
- ❖ $V_{breakdown} \sim 50\text{-}70\text{V}$
- ❖ $G \sim 10^6$

SiPM electrical model: a closer look



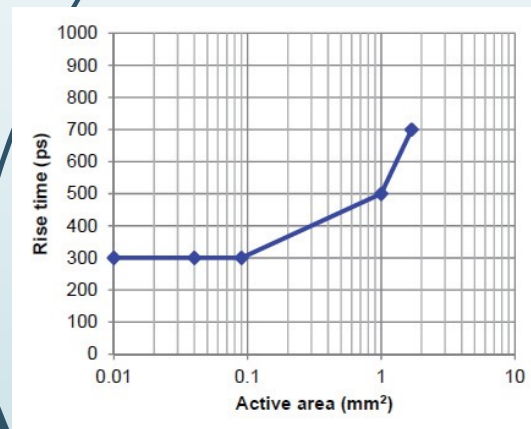
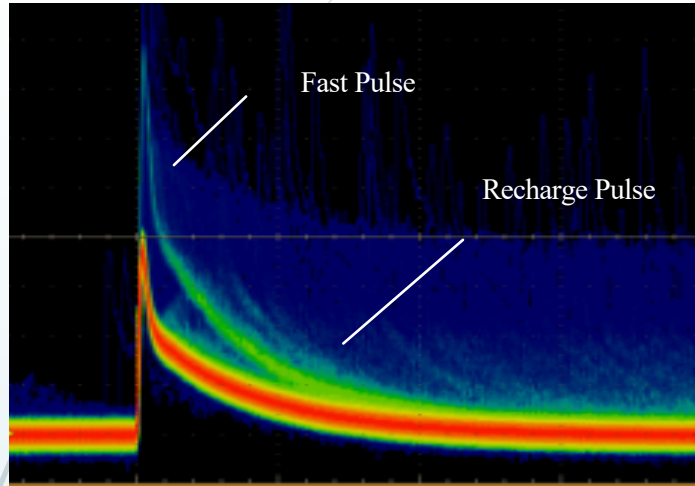
For a single cell (ref. 2, 2006)

- ❖ C_D = cell capacitance
- ❖ R_Q = quenching resistor
- ❖ C_q = stray capacitance of the quenching resistor
- ❖ R_S = space charge resistance + neutral regions ($\approx 1 \text{ k}\Omega$)
- ❖ R_b = substrate ohmic resistance
- ❖ C_g = stray capacitance of the cell grid to the substrate



For the full array (ref. 5, 2016), one cell “triggering” (fast response made easy as a “Dirac delta” of current)

SiPM electrical model: time development of the signal & parameters



Courtesy of HAMAMATSU Photonics

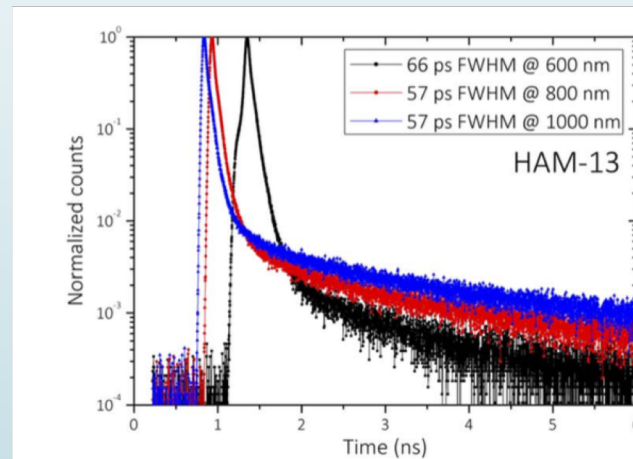
Ref.5

SiPM Hamamatsu S10931-050P
 $N = 3600$

V_{BD}	70.47 V
R_q	71.2 k Ω
R_b	22.9 Ω
C_d	74 fF
C_q	30 fF
C_g	40.8 pF

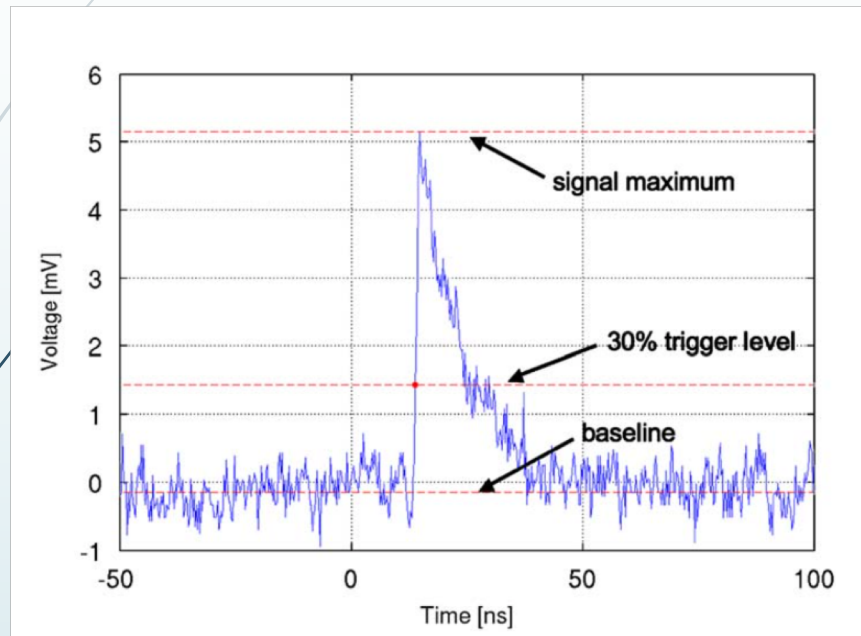
- ❖ Fast Pulse:
 $T_{FP} = R_S \times (C_D + C_Q) \approx$
- ❖ Recharge Pulse:
 $T_{RP} = R_Q \times (C_D + C_Q) \approx$

This is leading to an astonishing result: a Single Photon Timing resolution at the 60 ps level



	Hamamatsu 1.3 mm x 1.3 mm [S13081-050CS]
Name in this work	HAM-13
Total active area	1.69 mm ²
Fill factor	61%
Number of microcells	667
Peak PDE	35%
DCR	50 kcps
Breakdown voltage	53 V
Structure	p-on-n
Terminal capacitance	60 pF

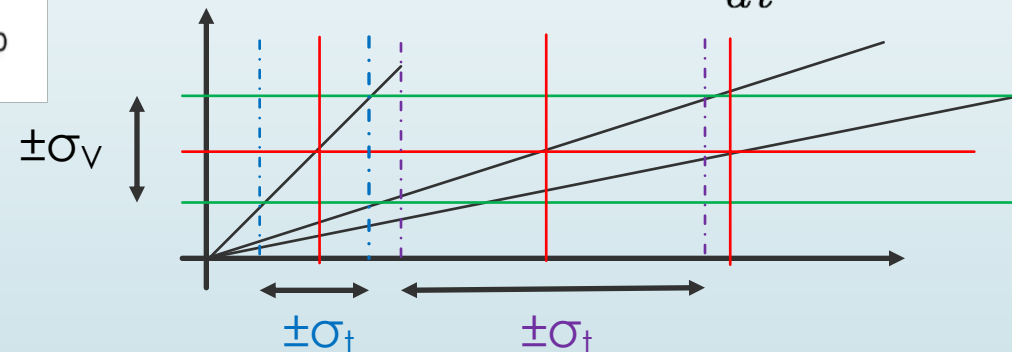
More about timing: impact of the **shape of the signal** and the **number of photons** (presuming they all come at once! It does not apply to timing with scintillation light) on time resolution



- ❖ The rise time of the signal obviously has an impact! Presuming a local linear dependence of the output voltage with time, you have:

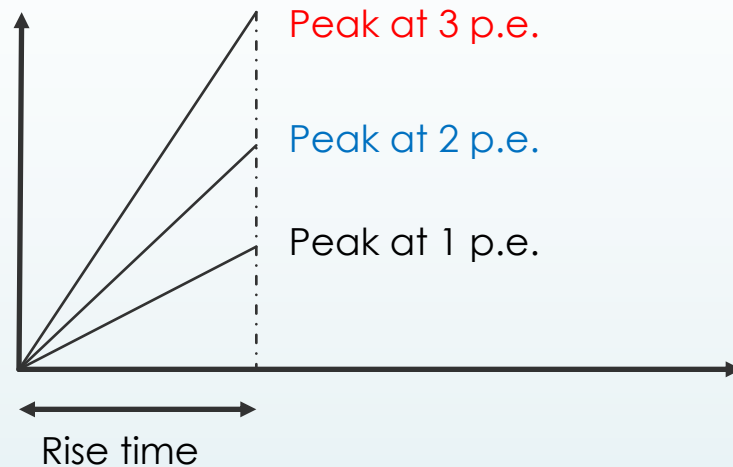
$$V = m \times t = \frac{dV}{dt} \times t$$

$$\implies \sigma_t = \frac{\sigma_V}{\frac{dV}{dt}}$$



* R. Vinke et al, Optimizing the timing resolution of SiPM sensors for use in TOF-PET detectors, Nuclear Instruments and Methods in Physics Research A 610 (2009) 188–191

- ❖ Presuming the rise time is defined by the sensor characteristics & front-end electronics and it is independent from the signal amplitude, it is clear that the LARGER the signal, the higher the slope:



The slope for N photo.electrons is

$$N \times \left. \frac{dV}{dt} \right|_{N=1}$$

$$\implies \sigma_N = \frac{\sigma_{1,slope}}{N}$$

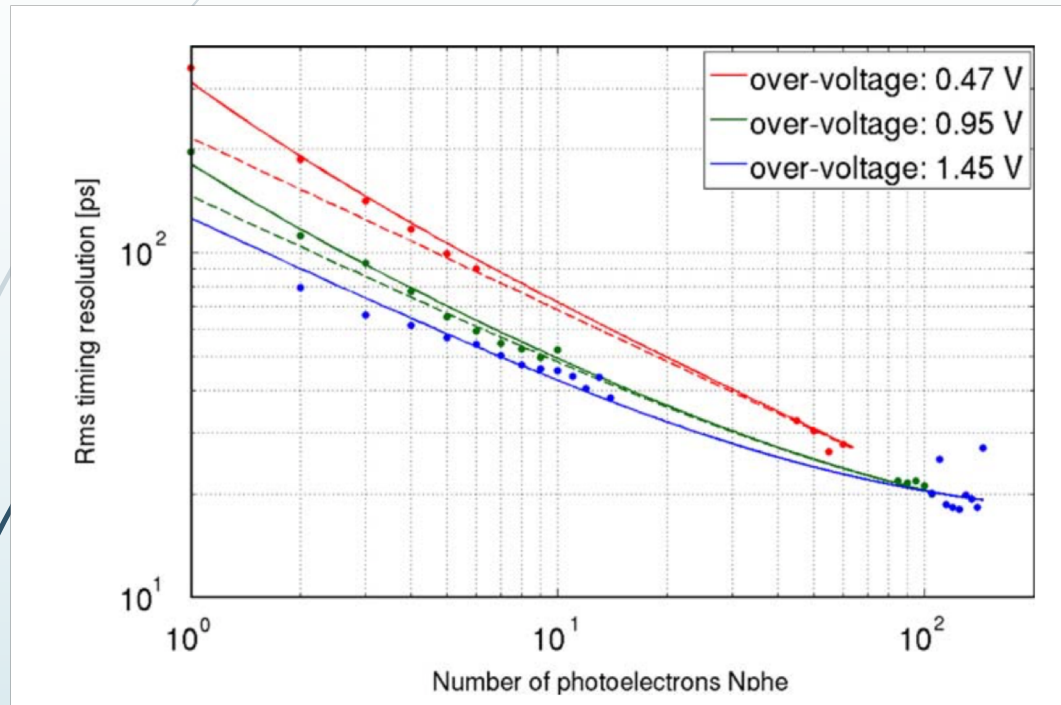
- ❖ Assuming to have N photo-electrons, the intrinsic fluctuation of the arrival time can be referred to the “mean photon”. And the spread of the mean of a series of N random variables is smaller than the spread of a single one by \sqrt{N} , namely:

$$\implies \sigma_{N,arrival} = \frac{\sigma_{1,arrival}}{\sqrt{N}}$$

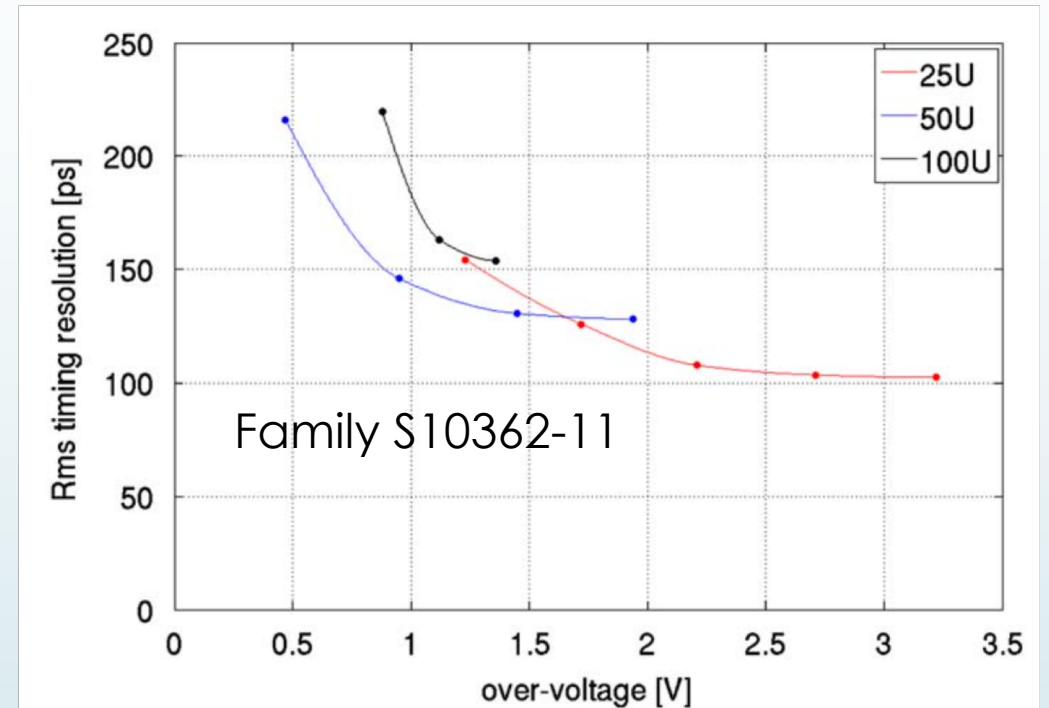
[a bit like saying that I time stamp every photon and I take the average..]

Summing (in quadrature) the different contributions, I have:

$$\sigma_{t,N}^2 = \sigma_0^2 + \frac{\sigma_{1,slope}^2}{N^2} + \frac{\sigma_{1,arrival}^2}{N}$$



Resolution vs. number of p.e.
(After Vinke et al.)

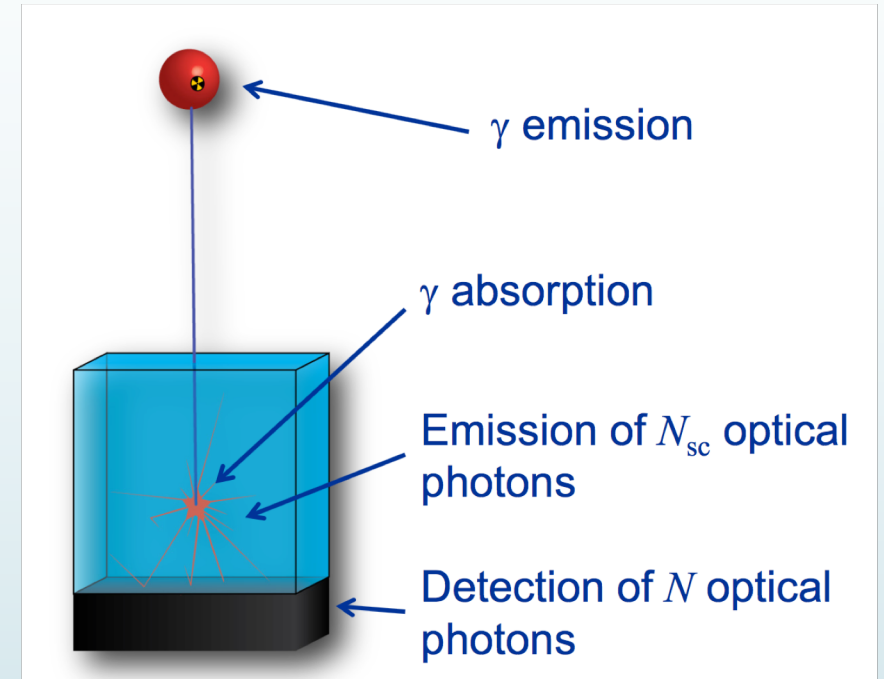


Intrinsic resolution for N=1
(After Vinke et al.)

Timing is actually a very serious topics and many bright minds devoted their time to it

A number of stochastic effects enter the game:

- ❖ The number of photons/event (particle interaction or light source pulse)
- ❖ The time distribution of the photons
- ❖ The optical photon dispersion in the crystal
- ❖ The spatial distribution of the photons on the sensor surface
- ❖ The time response of the sensor
- ❖ The shape of the signal
- ❖ The layout of the sensor
- ❖ The Time Stamping machine
- ❖ The “system noise”
- ❖ The algorithm (possibly not stochastic)

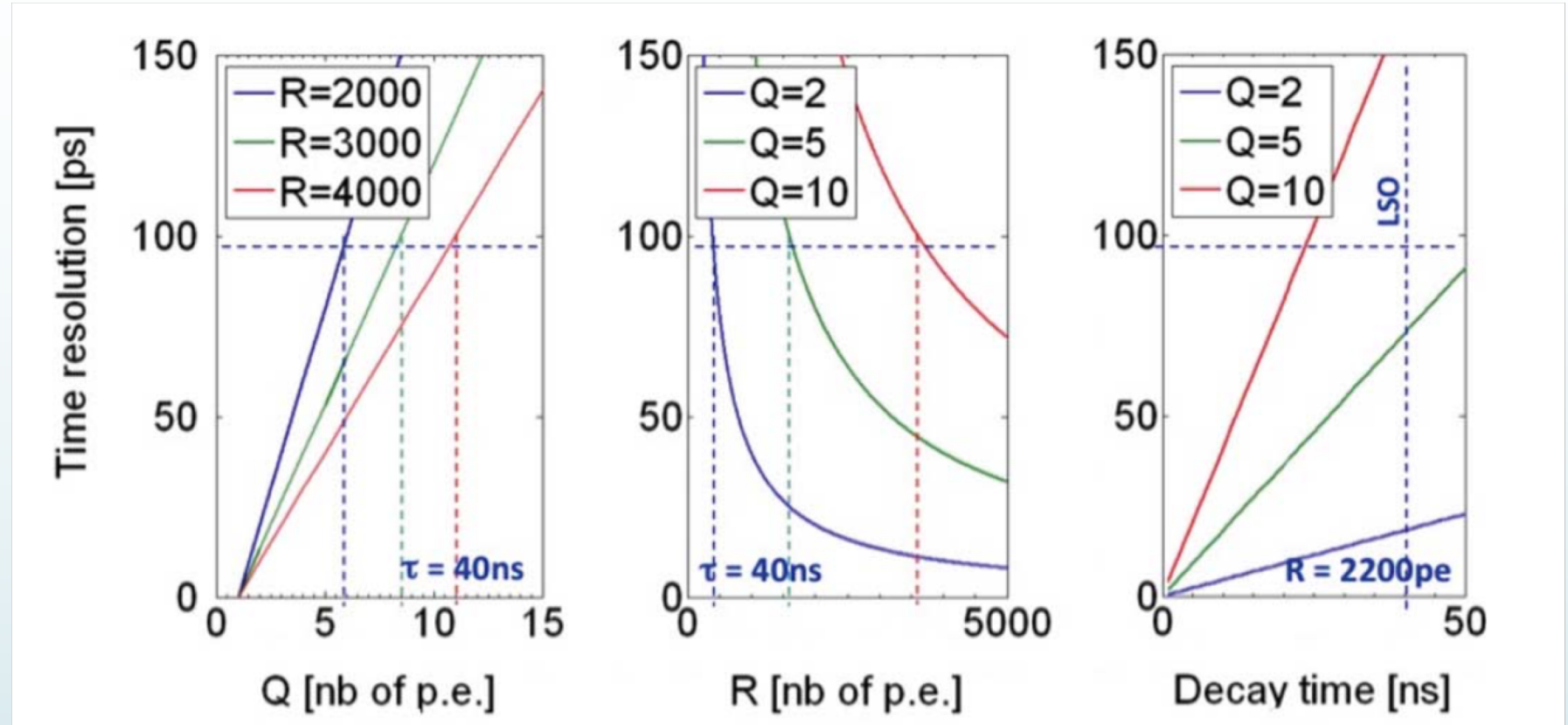


[credits for the drawing: Dennis Schaart, TU Delft]

It looks like the ideal situation for a Monte Carlo simulation but actually someone was so brave to tackle the problem analytically:

1. F. Acerbi et al. Characterization of Single-Photon Time Resolution: From Single SPAD to Silicon Photomultiplier, IEEE TNS – for technology/layout issues
2. R.F. Post & L.I. Schiff, Statistical limitations on the resolving time of a Scintillator counter, Physical Review, vol. 80, Issue 6, pp. 1113-1113 – a seminal paper (with unresolved doubts on my side)
3. S. Seifert, HT. Van Dam, D. Schaart, The lower bound on the timing resolution of scintillation detectors, Phys. Med. Biol. 57 (2012) 1797–1814 – an excellent paper! Formally correct, clear and useful
4. Leo H. C. Braga et al., A Time of Arrival Estimator Based on Multiple Timestamps for Digital PET Detectors, IEEE Nuclear Science Symposium and Medical Imaging Conference Record (NSS/MIC), 2012 – nice, even if the initial hp. could be discussed
5. S. Mandai et al., Timing optimization utilizing order statistics and multichannel digital silicon photomultipliers, OPTICS LETTERS / Vol. 39, No. 3 / February 1, 2014 - it shows the benefit of using multi-tagged photons
6. P. Lecoq et al., Factors Influencing Time Resolution of Scintillators and Ways to Improve Them [Nuclear Science Symposium Conference Record \(NSS/MIC\), 2009 IEEE](#), DOI: [10.1109/NSSMIC.2009.5402178](https://doi.org/10.1109/NSSMIC.2009.5402178) – it nicely addresses also the question of the light transport in crystals
7. Stephen Derenzo et al., Fundamental limits of scintillation detector timing precision, Phys. Med. Biol. 59 (2014) 3261–3286 – A Monte Carlo simulation ending up with a heuristic (horrible) formula
8. S. Vinogradov, Analytical model of SiPM time resolution and order statistics with crosstalk, Nucl. Instr. Methods A (2015), pp. 229-233 [<http://dx.doi.org/10.1016/j.nima.2014.12.010>]. A very good paper!

Three nice plots from ref. 6:

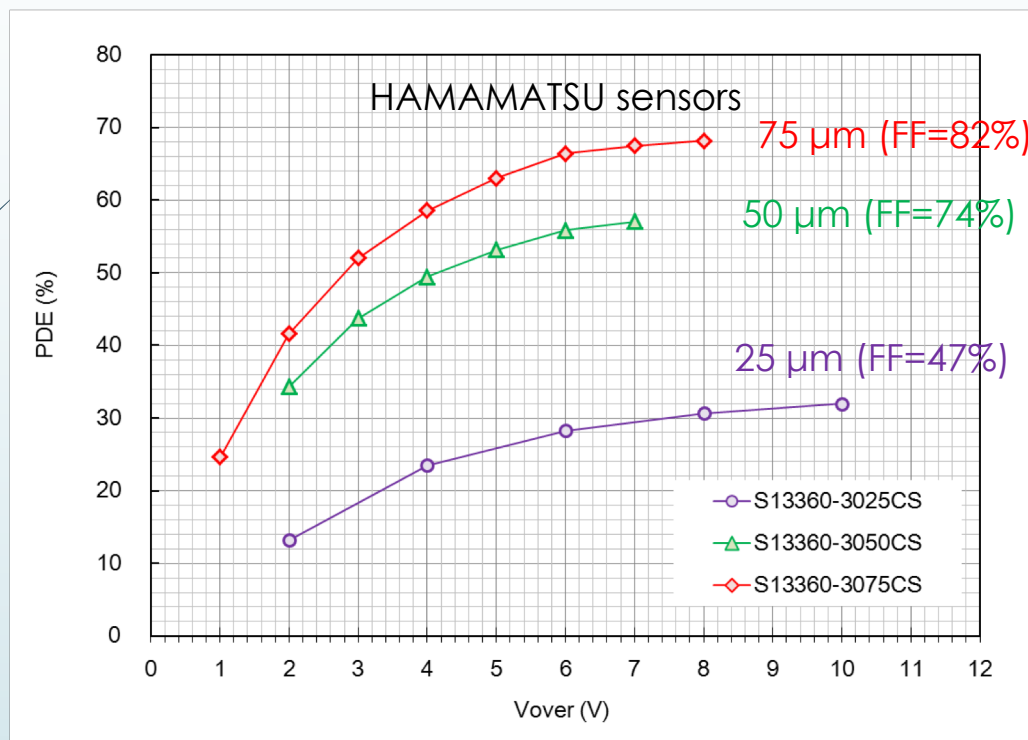


- ❖ R is the total light output
- ❖ Q is the threshold I set in photoelectrons \Rightarrow the LOWEST, the BEST

Photon Detection Efficiency:

$$\text{PDE} = n_{\text{p.e.}}/n_{\text{photons}}$$

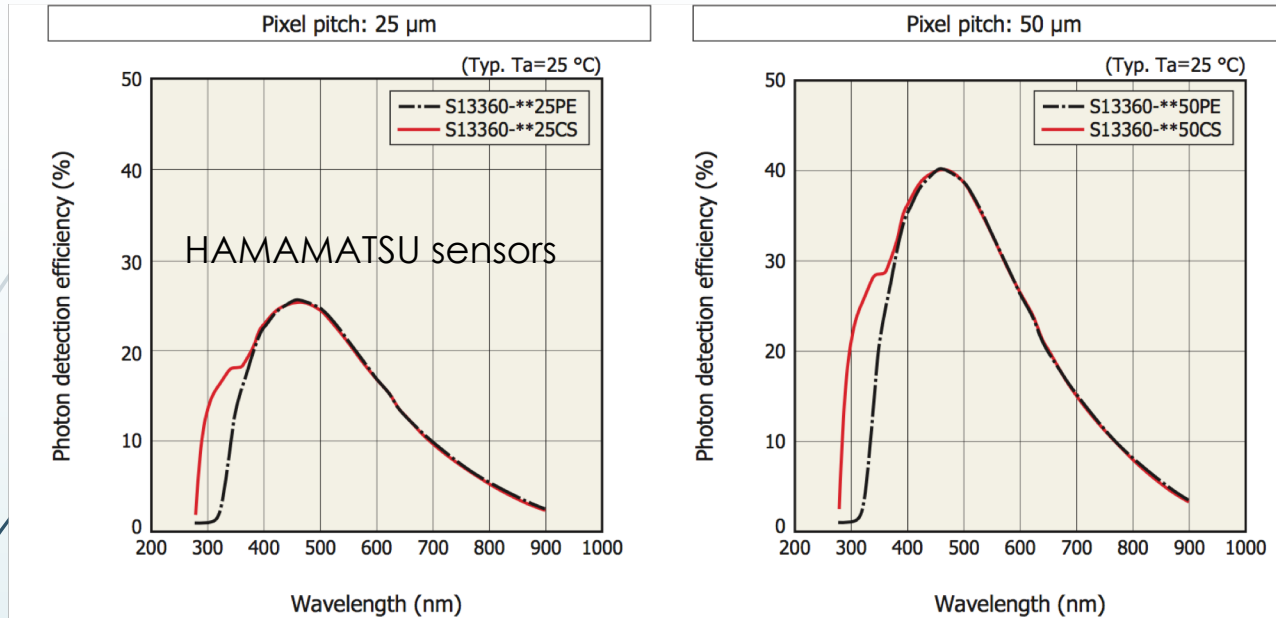
$$n_{\text{p.e.}} = n_{\text{photons}} \times [QE][\text{FillFactor}][P_{GM}]$$



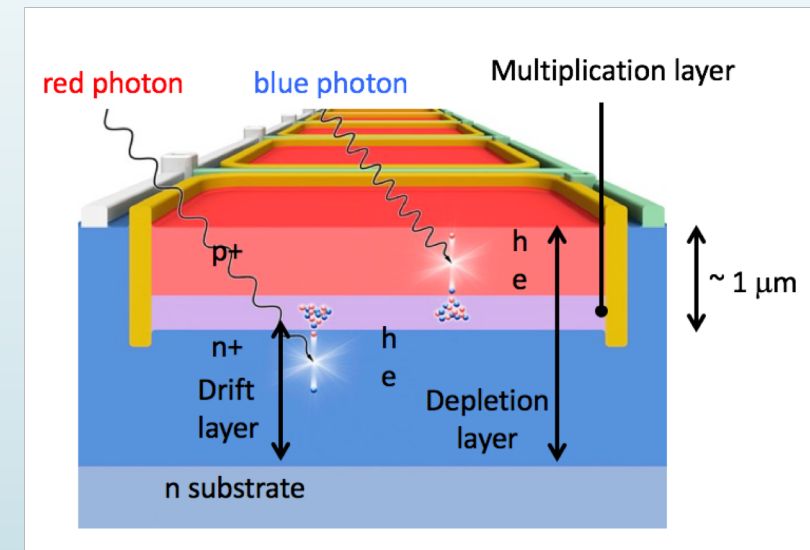
- ❖ QE = Quantum Efficiency (material properties)
- ❖ Fill Factor (FF) = fraction of sensitive area within the cell (technology)
- ❖ P_{GM} = triggering probability (physics, design and technology)

The variation of the ionization coefficients vs. over-voltage is the reason for the trend of the Photon Detection Efficiency (PDE)

Spectral response:



The variation vs wavelength results by the absorption properties of Silicon and the junction technology



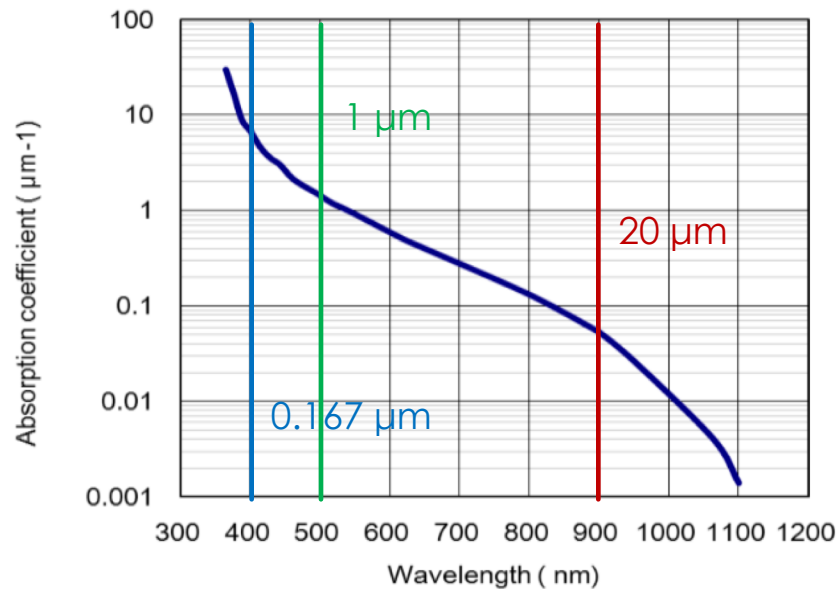
SiPM technology: what's behind the spectral response

1. Claudio Piemonte, Nuclear Instruments and Methods in Physics Research A 568 (2006) 224–232
2. Nagano et al., Development of new MPPC with higher NIR sensitivity and wider dynamic range, Internal note 2017
3. Oldham et al, IEEE 'TRANSACTIONS ON ELECTRON DEVICES, VOL.ED-19, NO. 9,SEPTEMBER 1972
4. McKay, Physical Review 94 (4) 877-884 (1954)

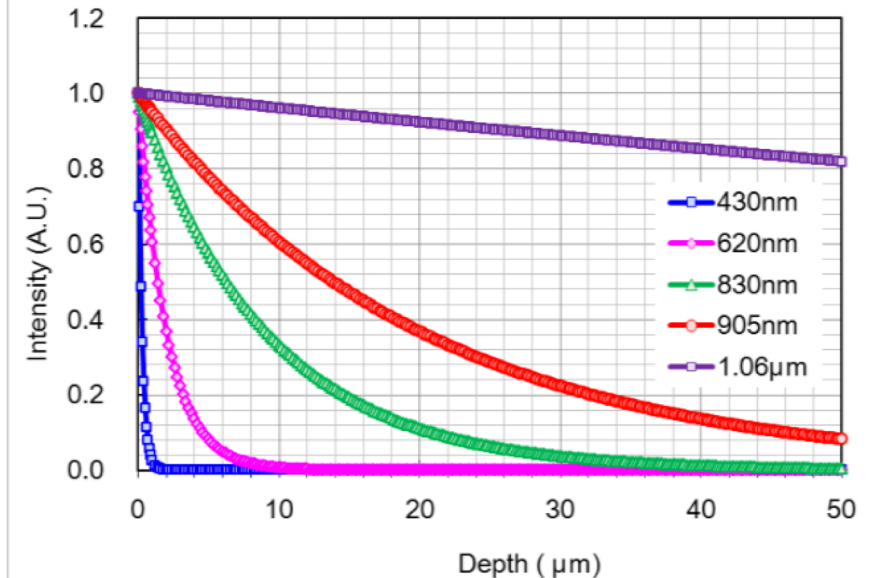
Light intensity in a medium drops exponentially: $I(x) = I_0 \times e^{-\mu x}$

1/e reduction (0.37) in:

(ref.2)



Absorption coefficient (μ) in [μm^{-1}] vs λ [nm]

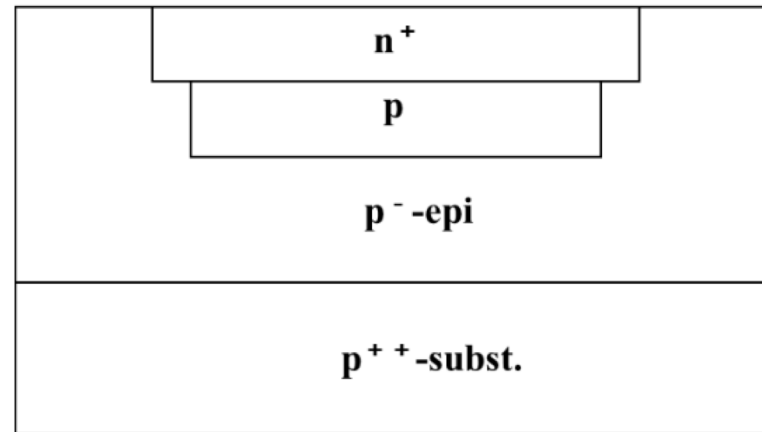


Light attenuation vs depth [μm]

I have to tailor my junction to maximize the probability to trigger an avalanche:

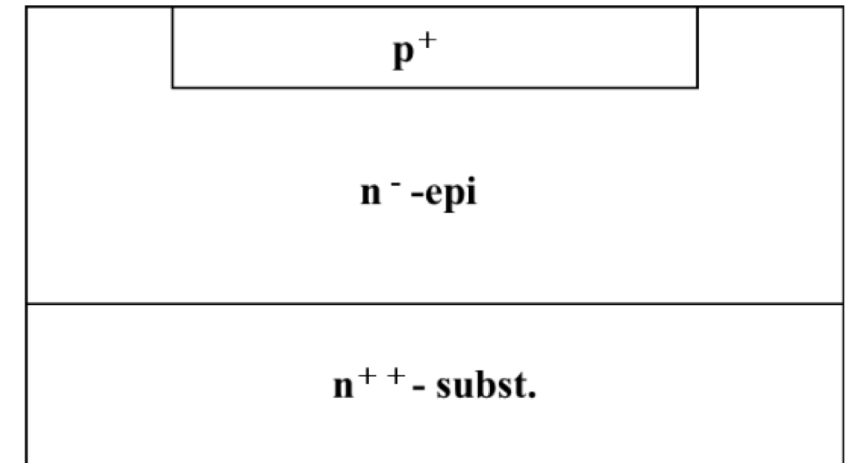
n-on-p junction:

- ❖ Not ideal for blue
- ❖ Good enough for green
- ❖ Bad for red



p-on- junction:

- ❖ Optimized for blue
- ❖ Fair enough for green
- ❖ Worse for red



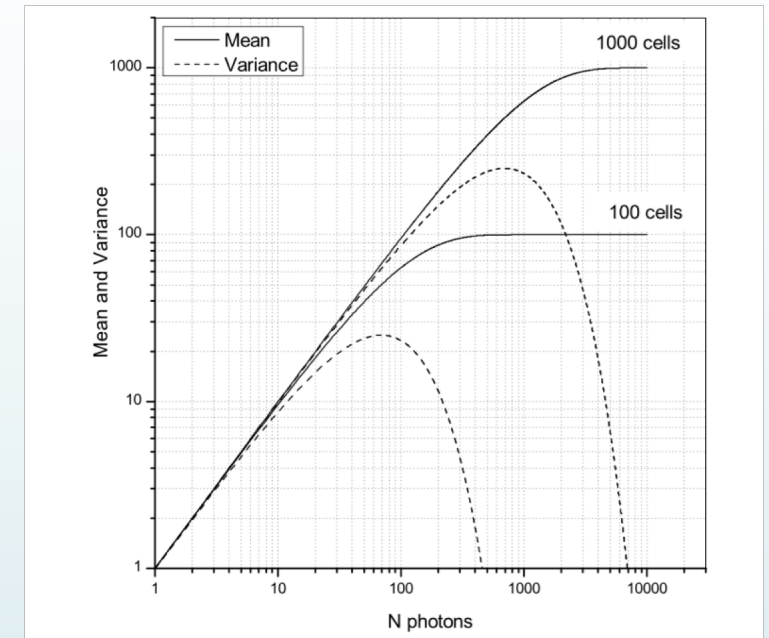
Stochastics effects affecting the sensor response

[actually introducing non-linearities]:

❖ Saturation [↓]:

$$N_{fired} = N_{cells} \times \left[1 - e^{-\frac{N_{photons} \times PDE}{N_{cells}}} \right]$$

K.E. Kuper et al. 2017 *JINST* **12** P01001

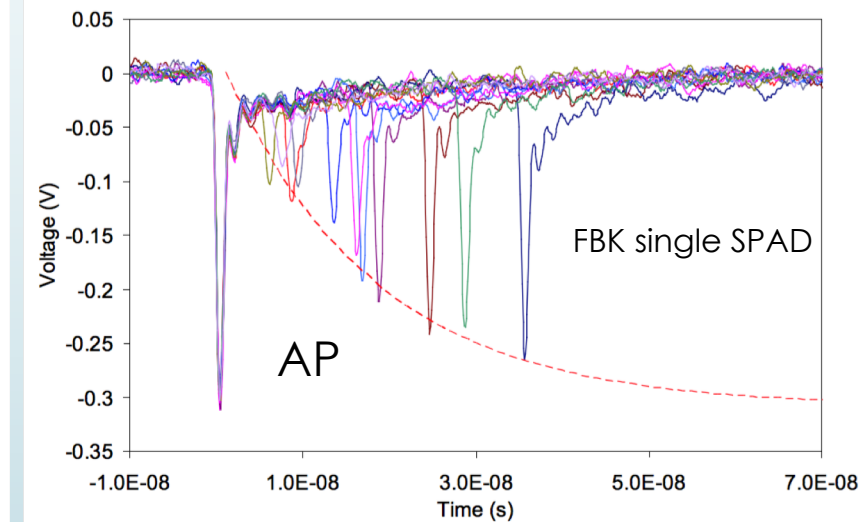
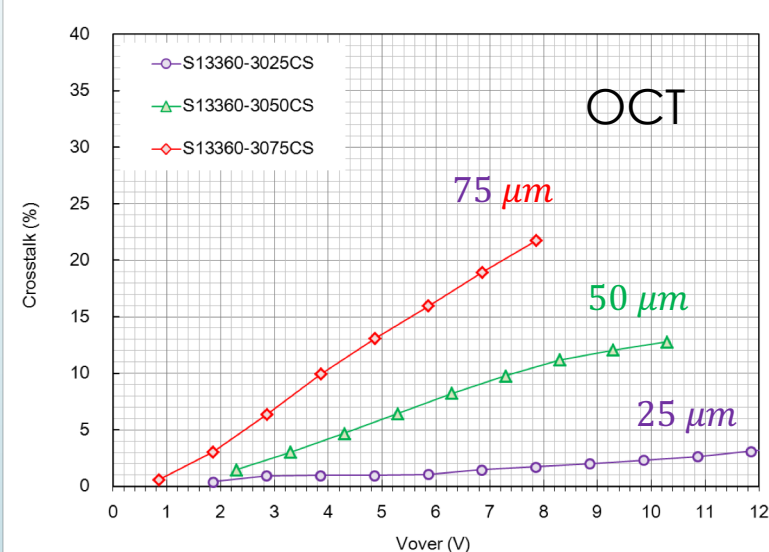
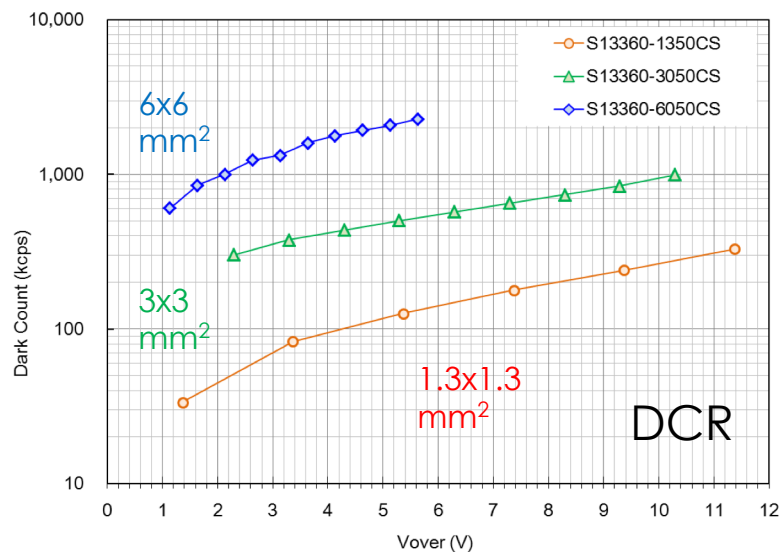


How do I get to this magic formula? In essence, it is a problem related to the finite number of cells & Geiger-Mueller process: as long as the probability of having more than one photo-electron (i.e. photon induced avalanche) in a single cell is not negligible, I can expect a deviation from the linearity in the response.

[look at the supplementary slides for a simple statistical exercise based on balls & baskets]

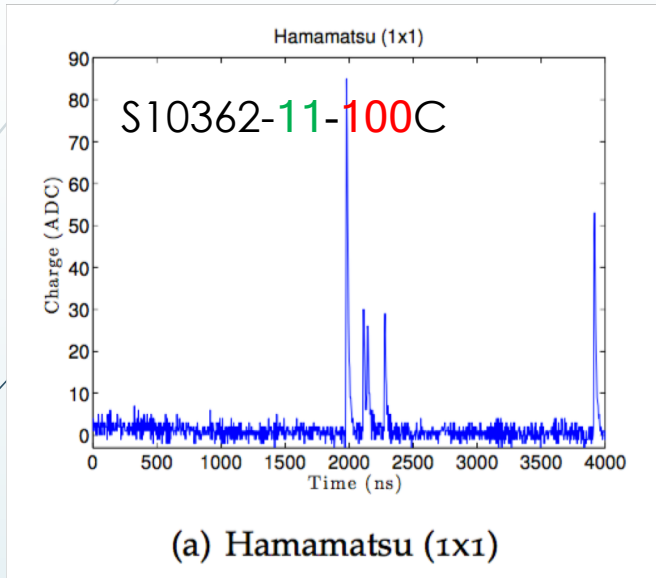
More Stochastic effects affecting the sensor response [actually introducing non-linearities]:

- ❖ **Dark Count Rate** [↑] (rate of avalanches randomly initiated by thermal generation of carriers): currently at the 60 kHz/mm² level
- ❖ **Optical Cross Talk** [↑] (secondary avalanches triggered by photons emitted during the primary event): currently < 10% at operating voltages
- ❖ **After-pulsing** [↑] (Delayed avalanches triggered by the release of a charge carriers that has been produced in the original avalanche and trapped on an impurity): ≈ 1% at operating voltages

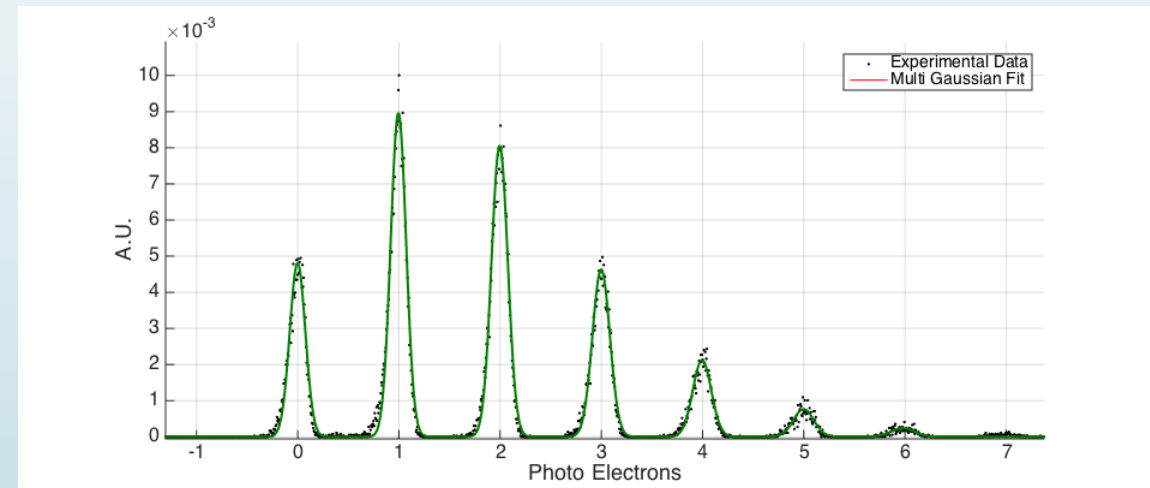
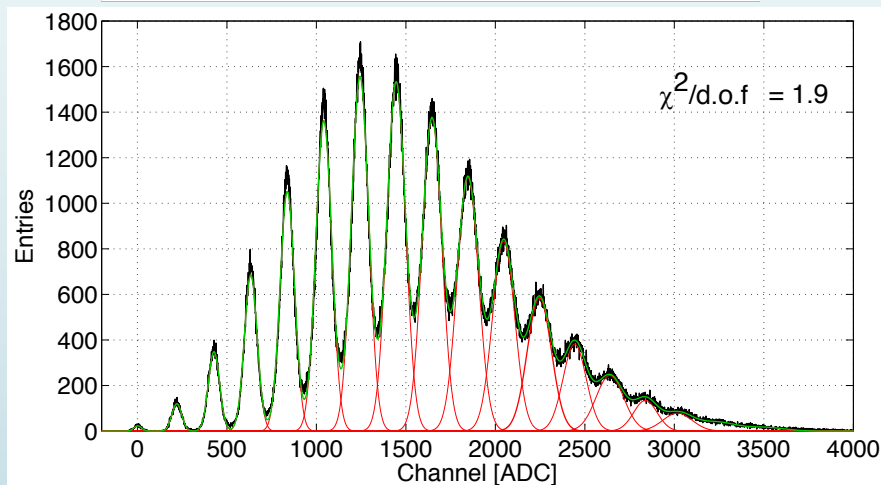
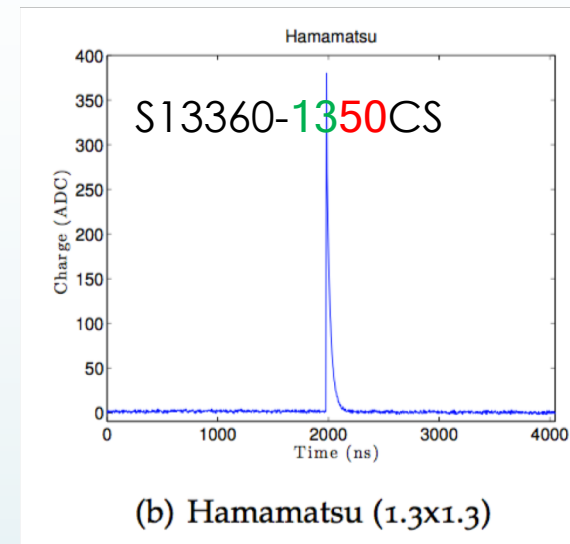


Since a picture is worth a thousand words:

An old sensor by HAMAMATSU (2008)



A new sensor by HAMAMATSU (2016)

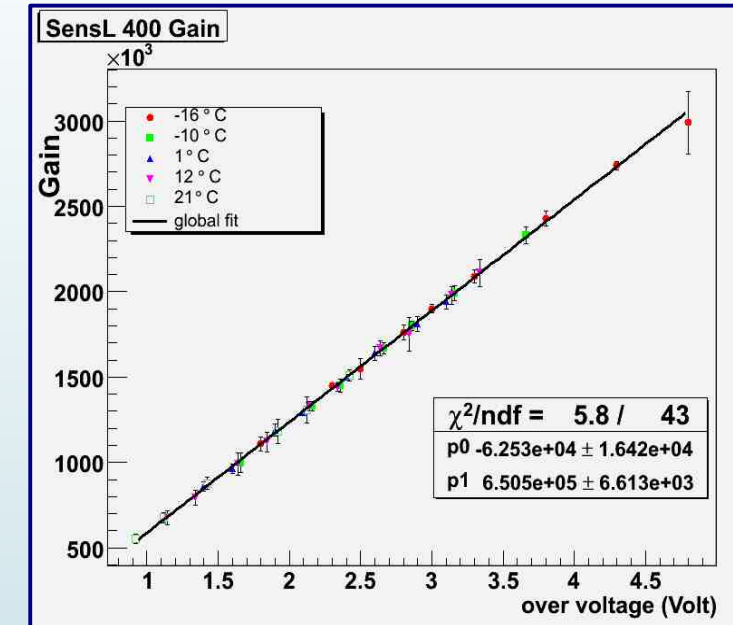
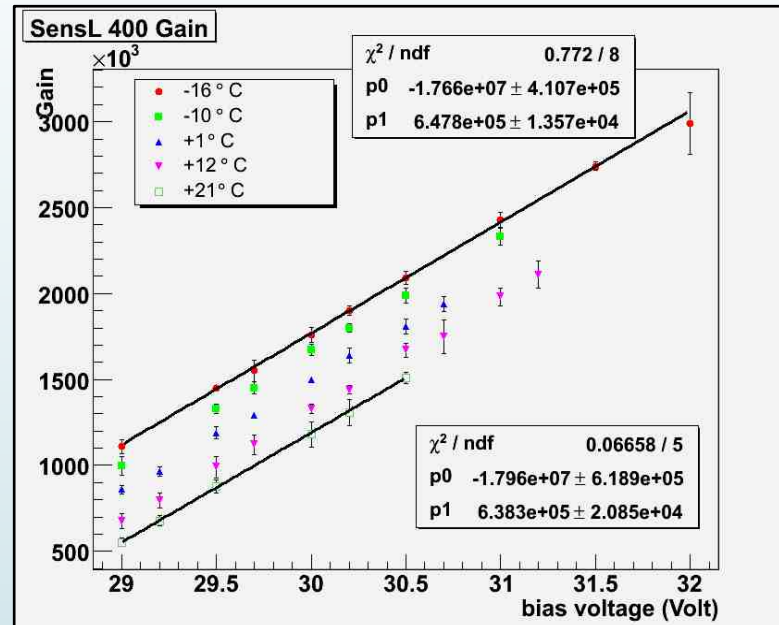
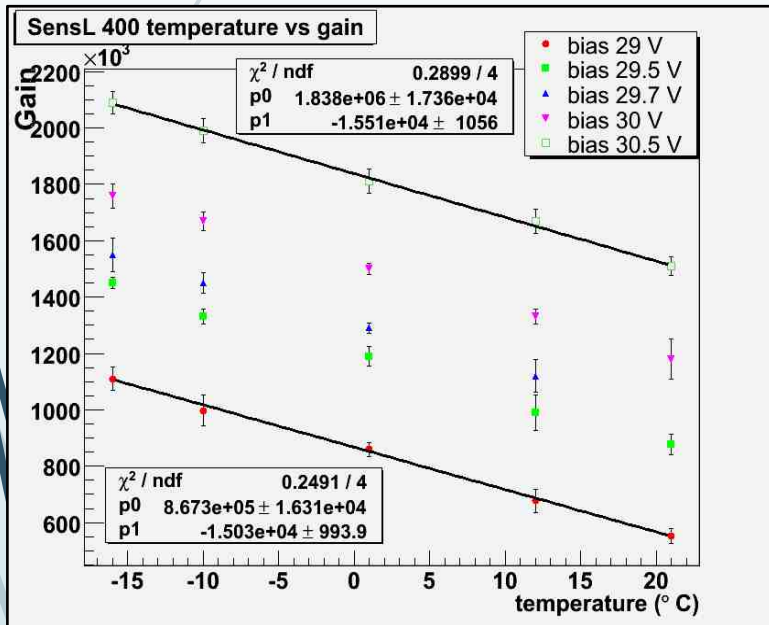


One more point: make it stable (against temperature stability)!

- C.R. Crowell, S.M.Sze, "TEMPERATURE DEPENDENCE OF IN SEMICONDUCTORS", APPLIED PHYSICS LETTERS 9, pag. 242, 1966
- C. Y. Chang, S. S. Chiu, and L. P. Hsu, "Temperature dependence of breakdown voltage in silicon abrupt P-N junctions," IEEE Trans. Elec- tron Devices, vol. 18, no. 6, pp. 391–393, 1971

$$V_{Br}(T) = V_{Br}(T_o) \times [1 - \beta(T - T_o)]$$

$$22 \text{ mV/}^\circ\text{K} < \beta < 55 \text{ mV/}^\circ\text{K}$$



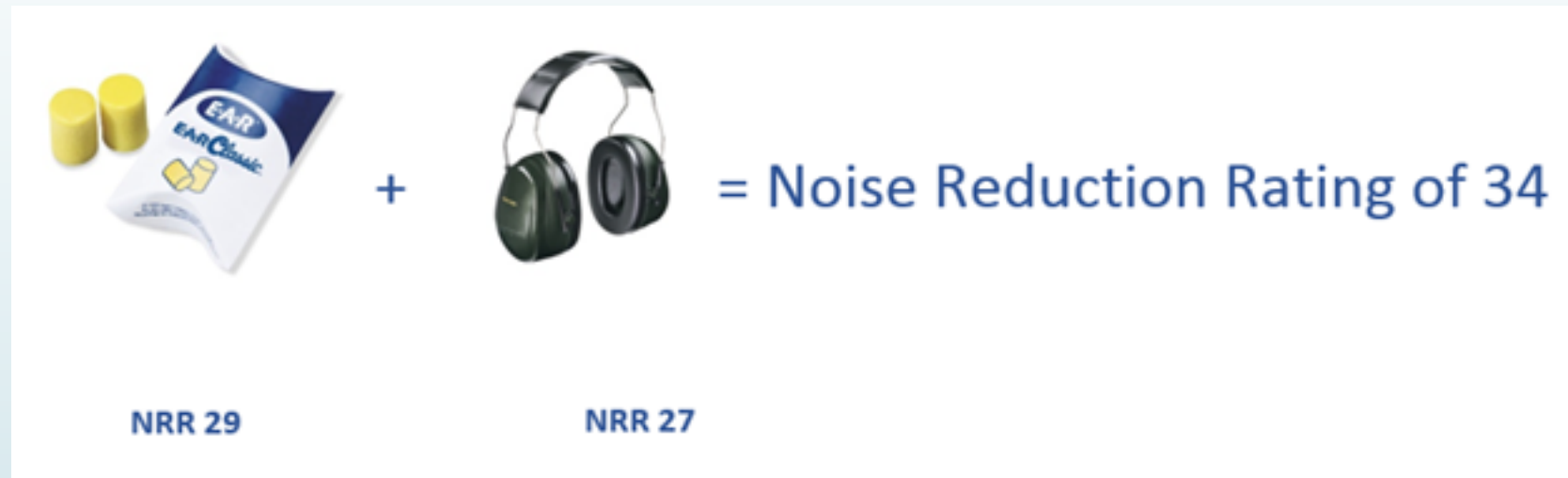
$$\frac{dV}{dT} = - \frac{dG}{dT} \frac{1}{\frac{dG}{dV}}$$

What's Next?



Trends in the R&D (user's driven, steered by the companies):

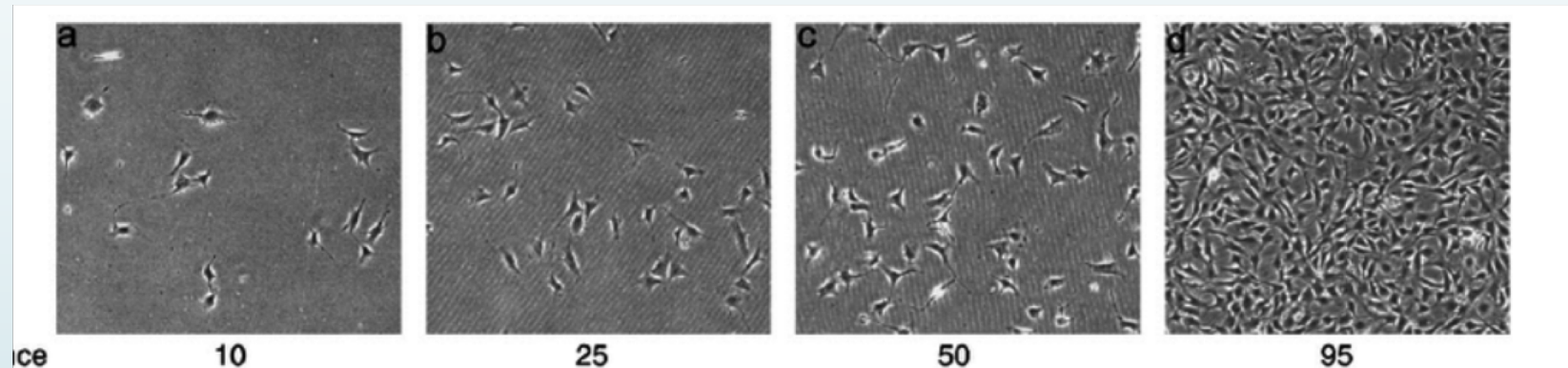
- Make it (more) quiet (decrease the stochastic terms)



The diagram illustrates the additive effect of different noise reduction methods. On the left, there is a package of yellow earplugs labeled 'EAR Classic' with two individual earplugs shown next to it, with the text 'NRR 29' below. In the center is a plus sign '+'. To the right of the plus sign is a pair of black over-ear headphones, with the text 'NRR 27' below. To the right of the headphones is an equals sign '=' followed by the text 'Noise Reduction Rating of 34'.

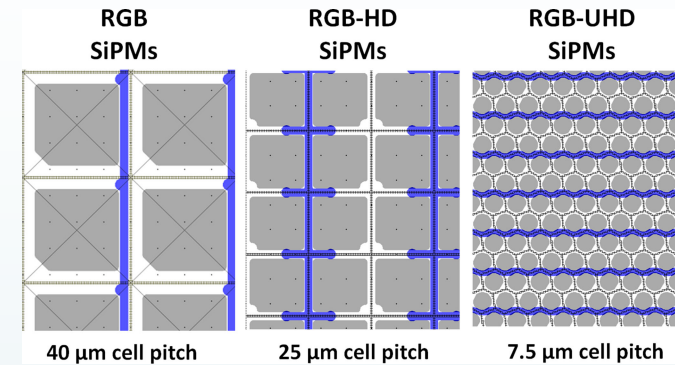
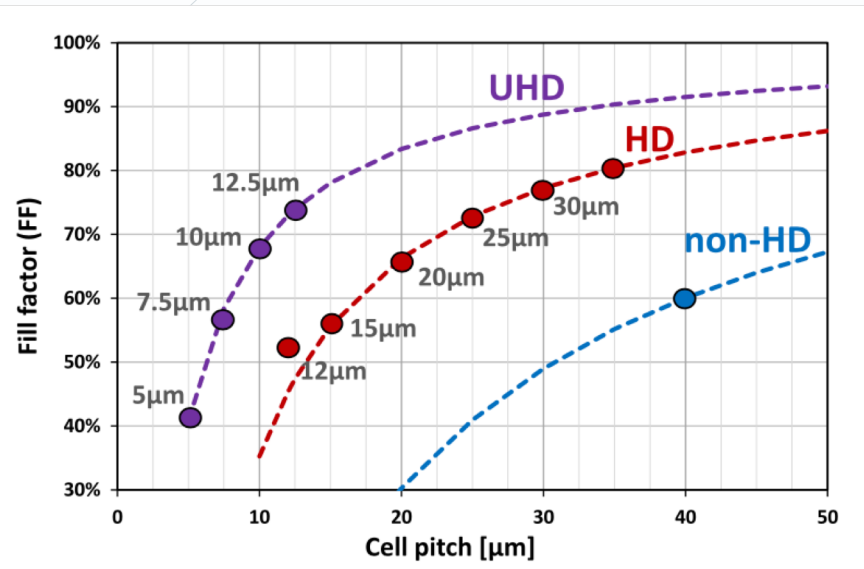
Trends in the R&D (user's driven, steered by the companies):

- Increase the cell densities (extend the dynamic range)

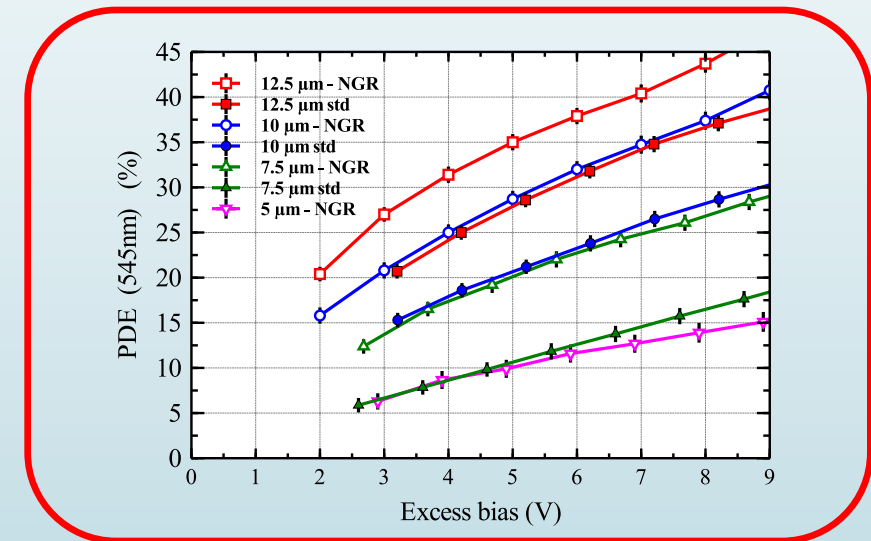
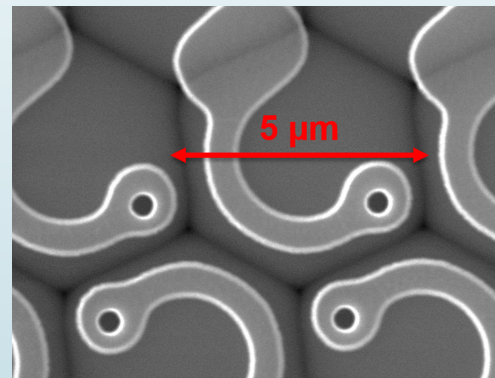
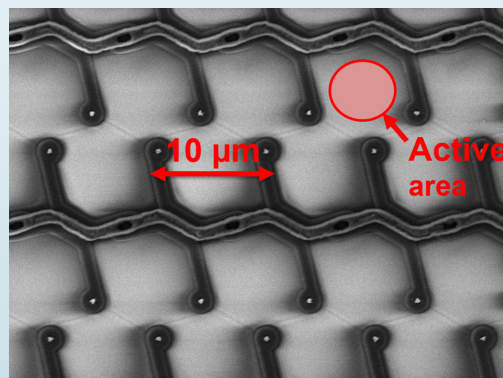


Latest from Fondazione Bruno Kessler in Trento (Italy)

F. Acerbi et al., IEEE JOURNAL OF SELECTED TOPICS IN QUANTUM ELECTRONICS, VOL. 24, NO. 2, MARCH/APRIL 2018



Cell pitch	5 μm	7.5 μm	10 μm	12.5 μm
Cell area [μm ²]	21.6	48.7	86.6	135
Cell density [cells/mm ²]	46190	20500	11500	7400
Cell Fill Factor	40.9%	57%	68%	75%



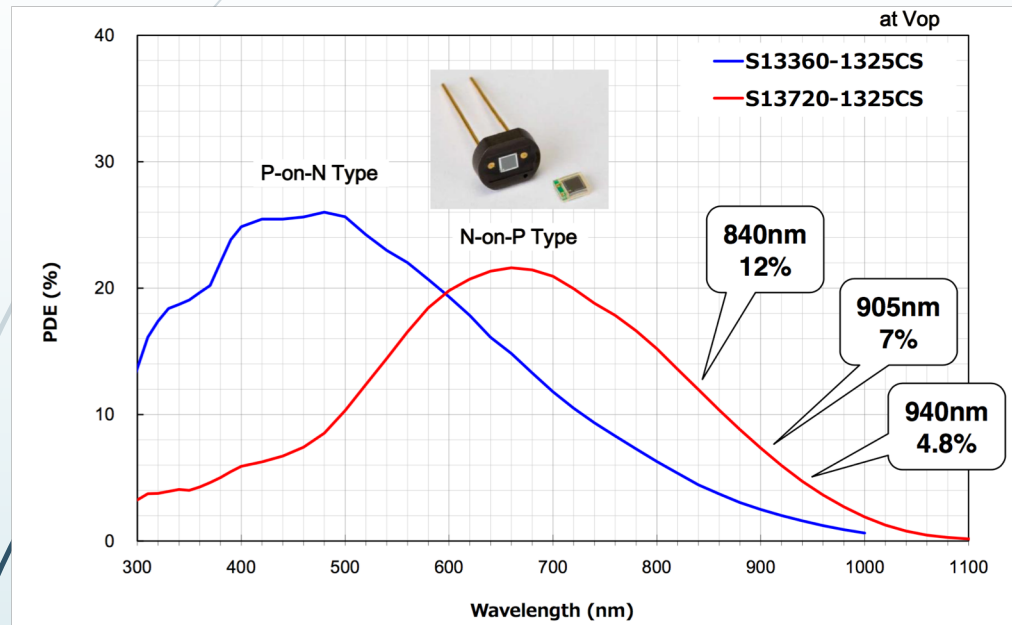
Trends in the R&D (user's driven, steered by the companies):

- Push the sensitivity a bit to the right (NIR)

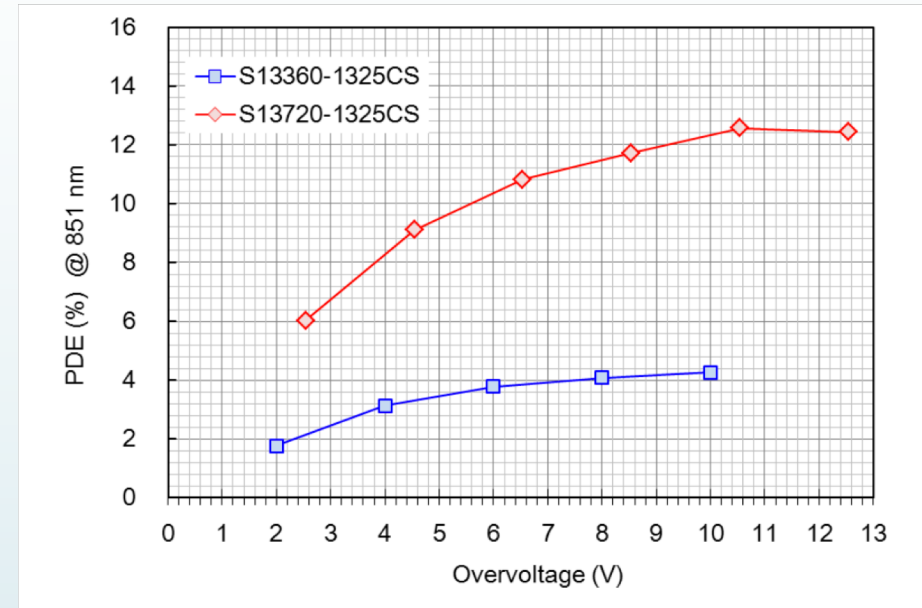


- ... and to the left (NUV)

Where are we today (2018)? The latest from HPK on the IR side



Photon Detection Efficiency vs wavelength



PDE vs overvoltage

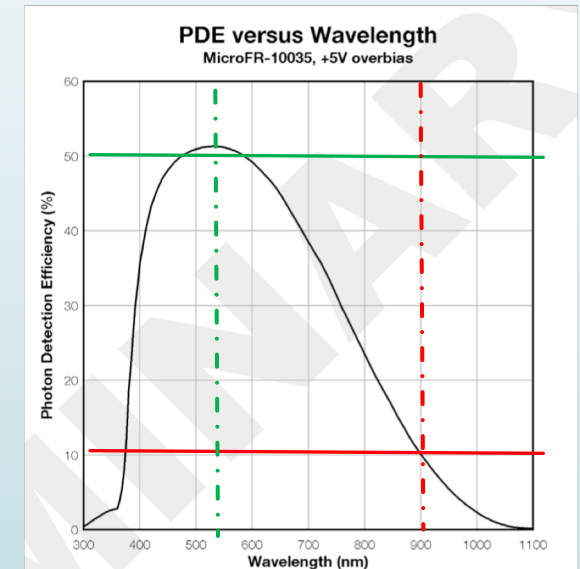
Where are we today (2018)? @SensL:

Sensor Size	Microcell Size	Parameter ¹	Overvoltage	Min.	Typ.	Max.	Units
1mm	10μm	@ 635nm	Vbr + 5.0V		30		%
		@ 780nm			18		%
		@ 905nm			8		%
	20μm	@ 635nm			39		%
		@ 780nm			24		%
		@ 905nm			10		%
	35μm	@ 635nm			47		%
		@ 780nm			29		%
		@ 905nm			12		%

Available products (R series)

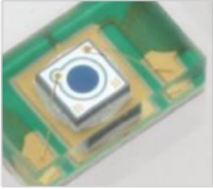
DCR \approx 70 kHz / mm² @5V_{over}

50%

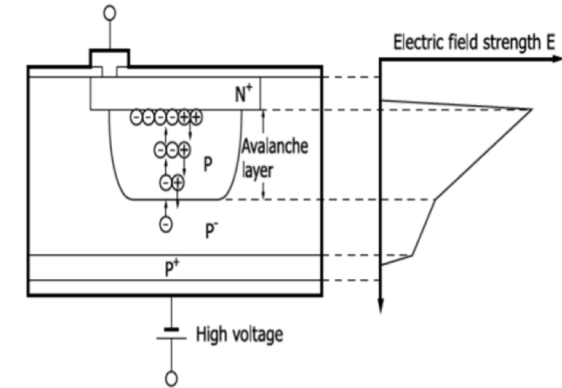
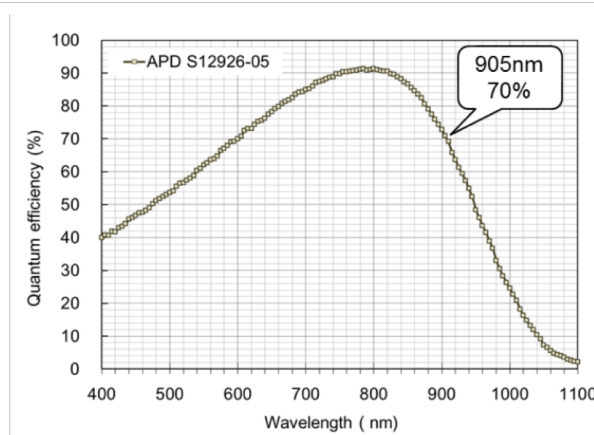


Worth fighting against APD?

APD
S12926-05



$V_{op} = 160\text{ V}$
 $\lambda_p = 800\text{ nm}$
 $QE = 70\% (905\text{ nm})$
 $M = 100$
 $\Delta T = 1.1\text{ V/}^\circ\text{C}$



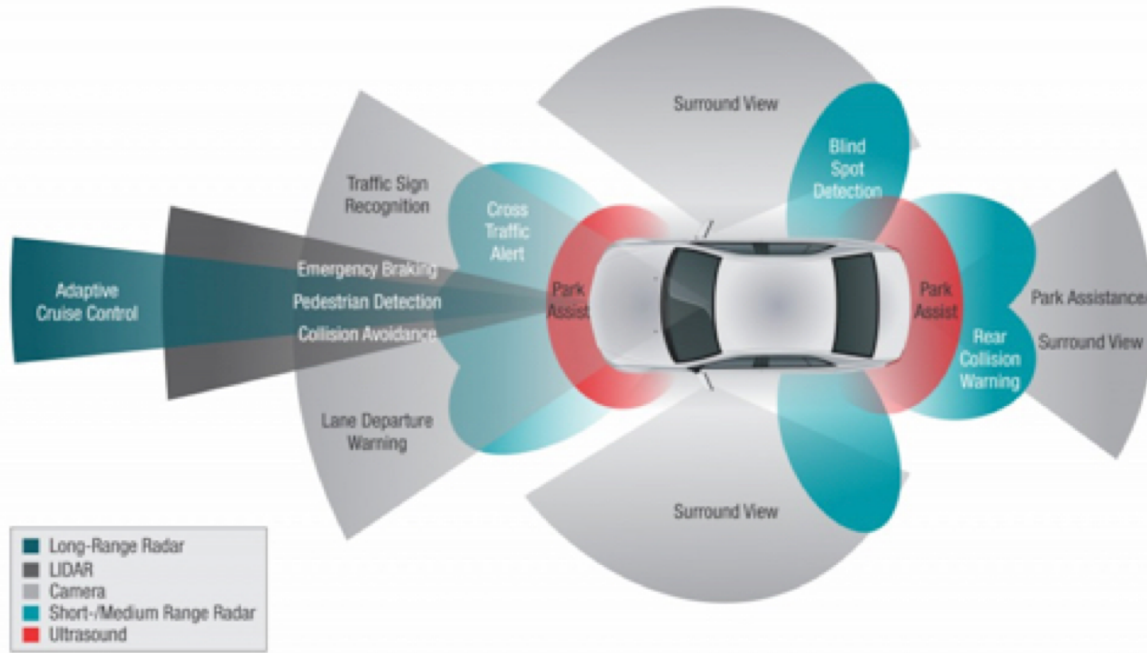
- ❖ M is the multiplication factor, 10^{-4} lower than SiPM
- ❖ The QE is 6 times higher than the PDE in SiPM
- ❖ The biasing voltage is ≈ 5 times higher than SiPM
- ❖ the sensitivity is at the 100 photon level ("range extender")

MindTheNumbers: if I scale down 35W/A by a factor 6 and I scale it up by a factor 10 000, I get 60kA/W, even if SensL claims these are measured figures.

	PiN Photodiode	APD	SiPM/SPAD
Gain	1	10^2	10^6
Operating voltage	5V	100V - 1000V	30V
Responsivity at 905nm	0.3A/W	35A/W	530kA/W
Implementation challenges	- External amplification limits signal to noise ratio (SNR) and bandwidth	- External amplification limits bandwidth and low return signal detection - Sensor to sensor non-uniformity and internal gain excess noise factor - High volume cost due to non-standard CMOS fabrication processes	- Ambient light rejection $\pm 25\text{nm}$ bandpass filter reduces light by a factor 25

SensL

Certainly YES!



But do not forget ranging is also important for other markets:

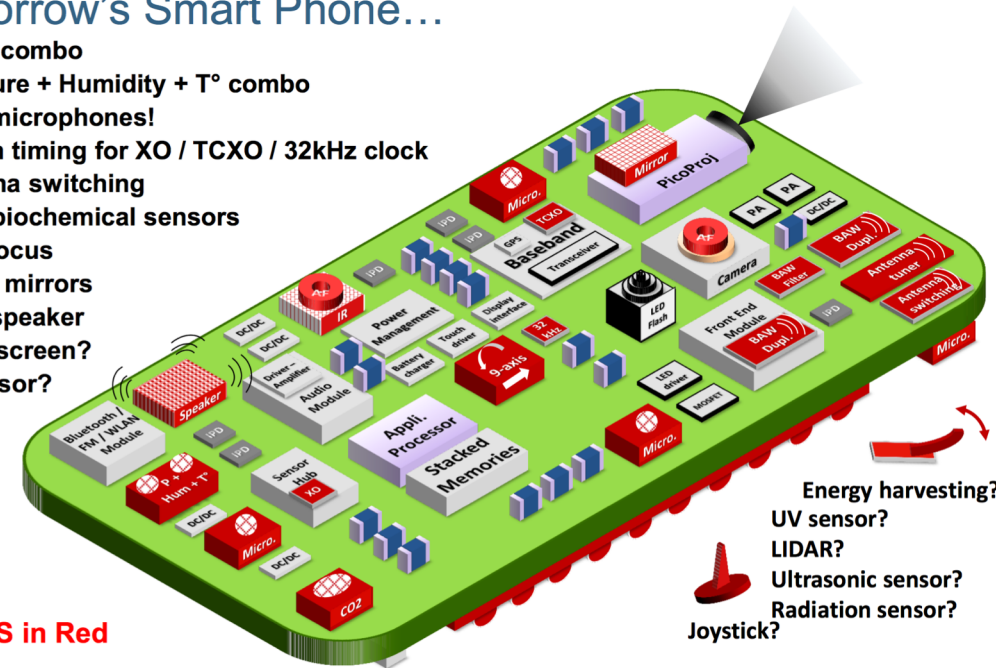
- ❖ Landscape topography
- ❖ Industrial applications
- ❖ Military

Look at the INSPEX H2020 project on obstacle detection to see what's going on at EU level

Tomorrow's Smart Phone...

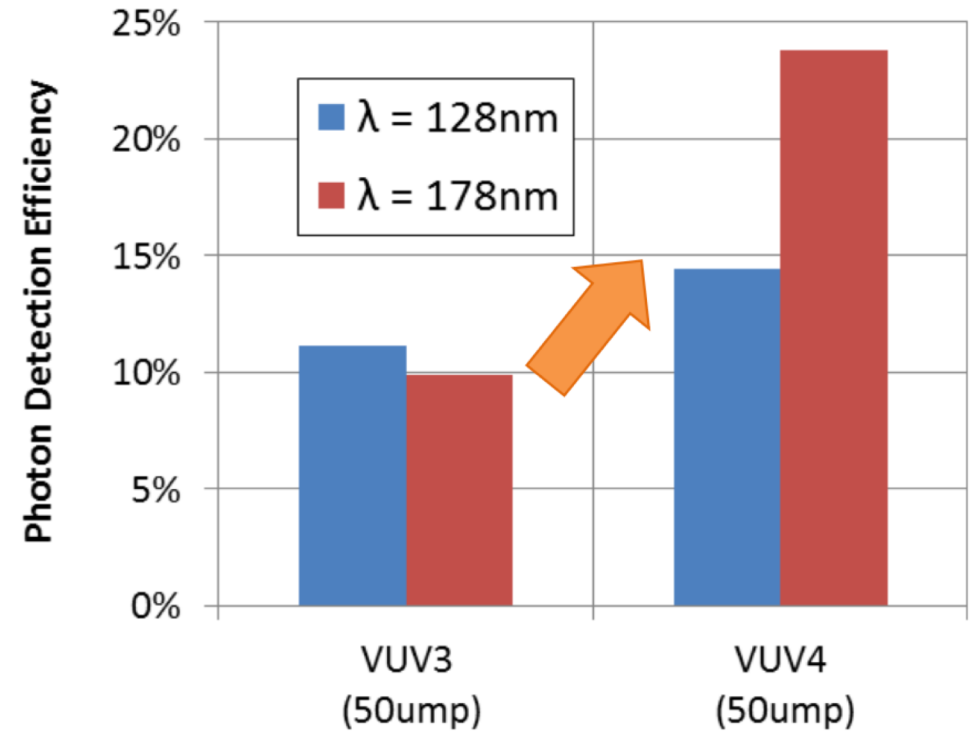
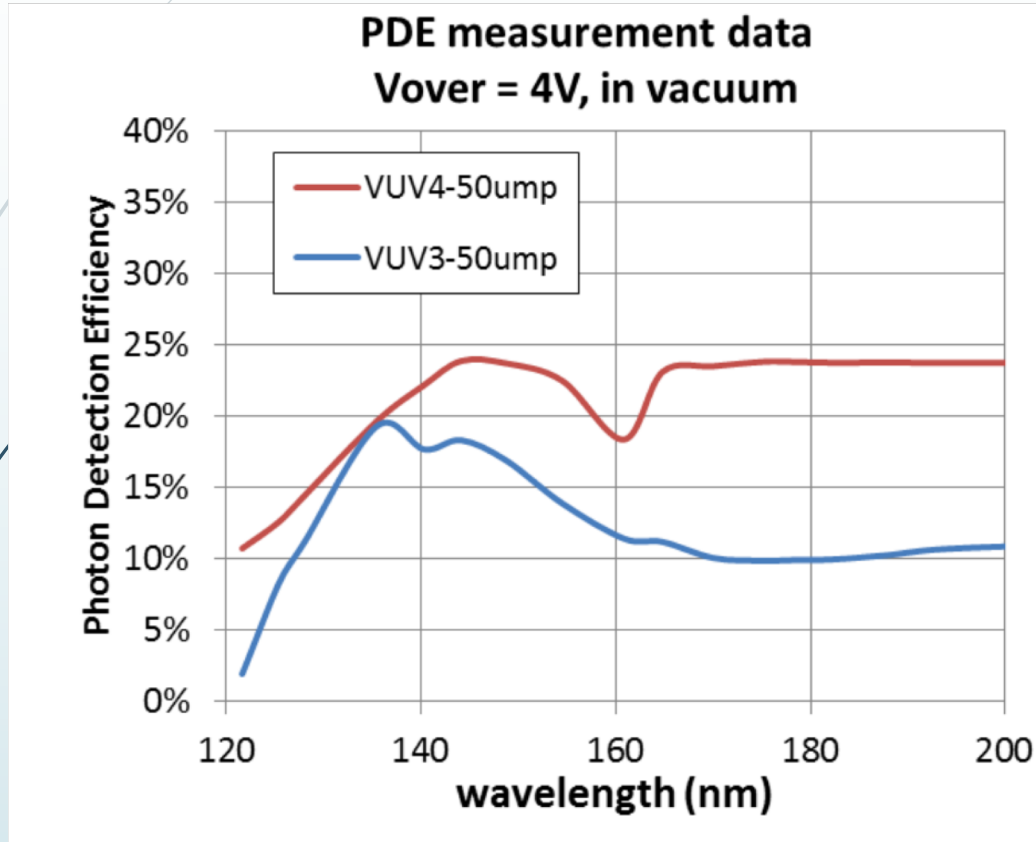
- 9-axis combo
- Pressure + Humidity + T° combo
- More microphones!
- Silicon timing for XO / TCXO / 32kHz clock
- Antenna switching
- Gas / biochemical sensors
- Auto-focus
- MEMS mirrors
- Microspeaker
- Touchscreen?
- IR sensor?

MEMS in Red

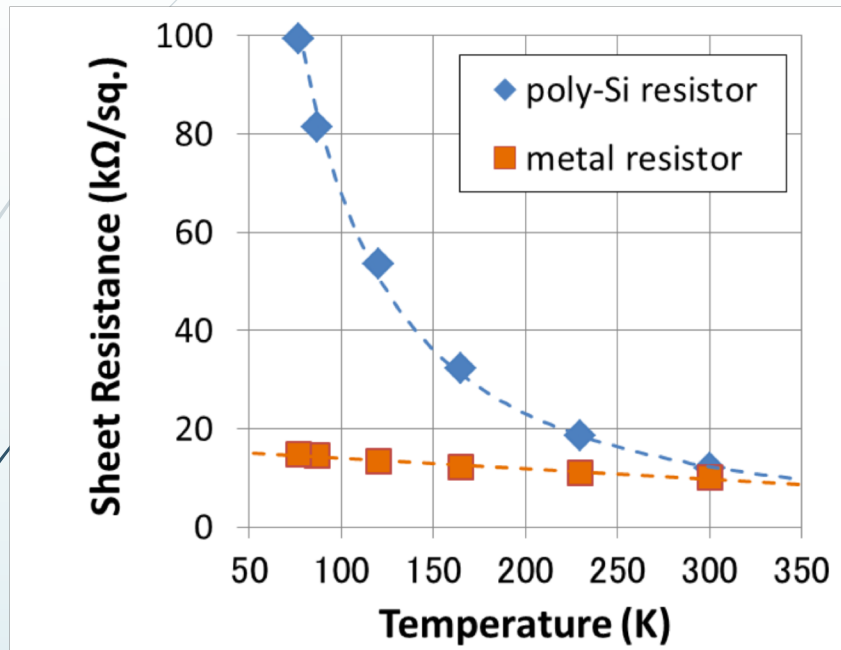


(Source: Yole Development - MEMS for Cell Phones & Tablets, July 2013)

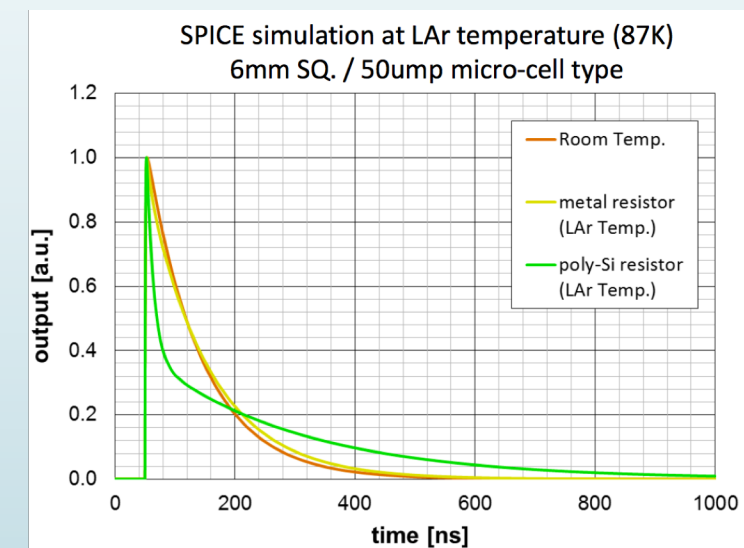
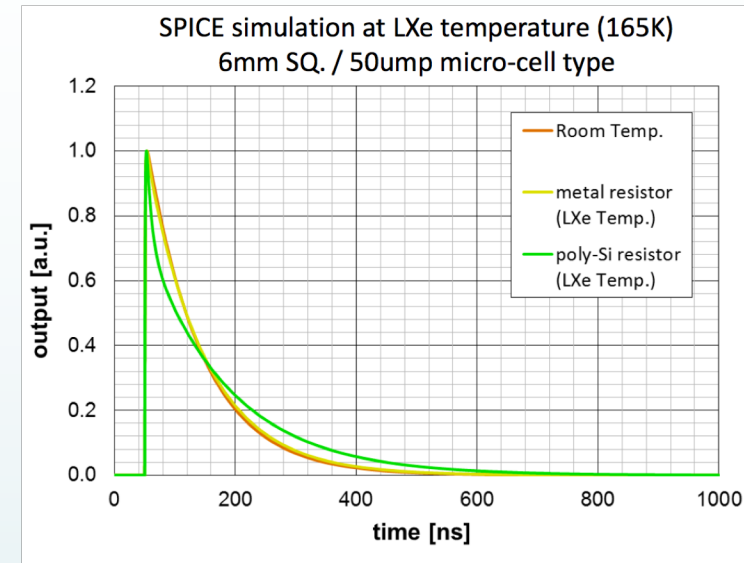
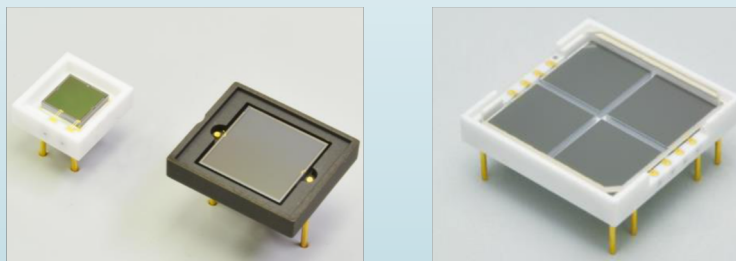
The latest from HPK: on the UV side



VUV enhanced sensitivity goes along with good functionality at cryo-T:



S13370 and S13361 series, available in ceramic package with high radio purity



Trends in the R&D (user's driven, steered by the companies):

- Integrate a bit of intelligence on board





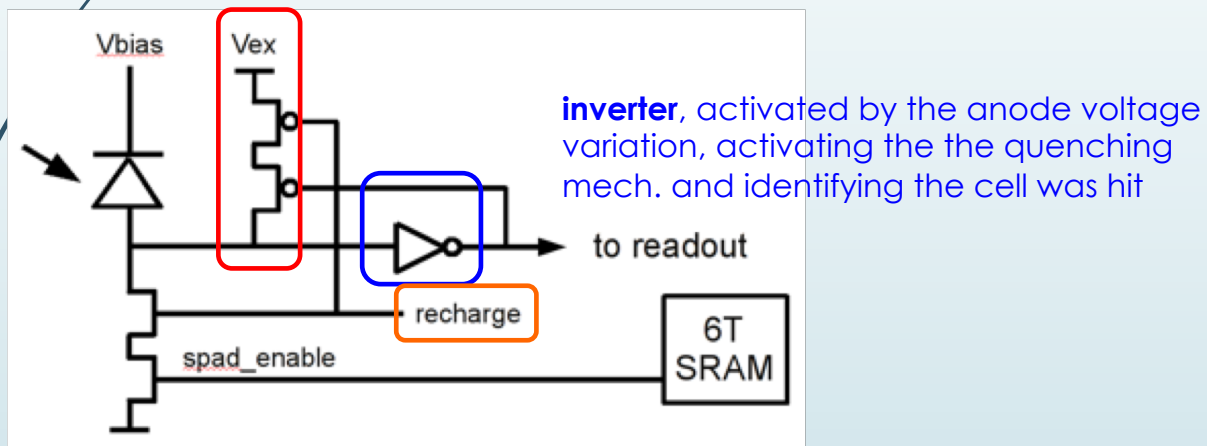
Philips Digital Photon Counting

<http://www.digitalphotoncounting.com>

- IEEE-NSS Conference record 2009 & 2010 (Thomas Frach)
- JINST 7 (2012) C01112
- D. Schaart et al., NIM A 809 (2016) 31-52

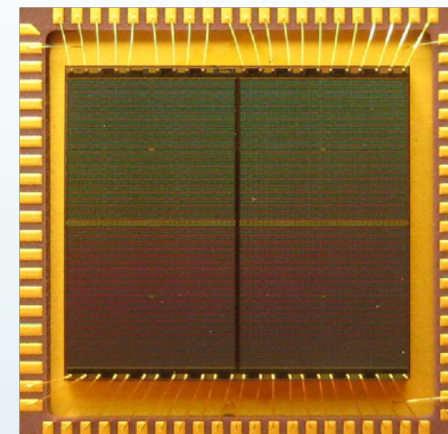
Put a bit of intelligence on board and turn the SiPM into a genuine DIGITAL device:

Active quenching, forcing the anode to the breakdown voltage



Quick recharge transistor

The 2009 chip

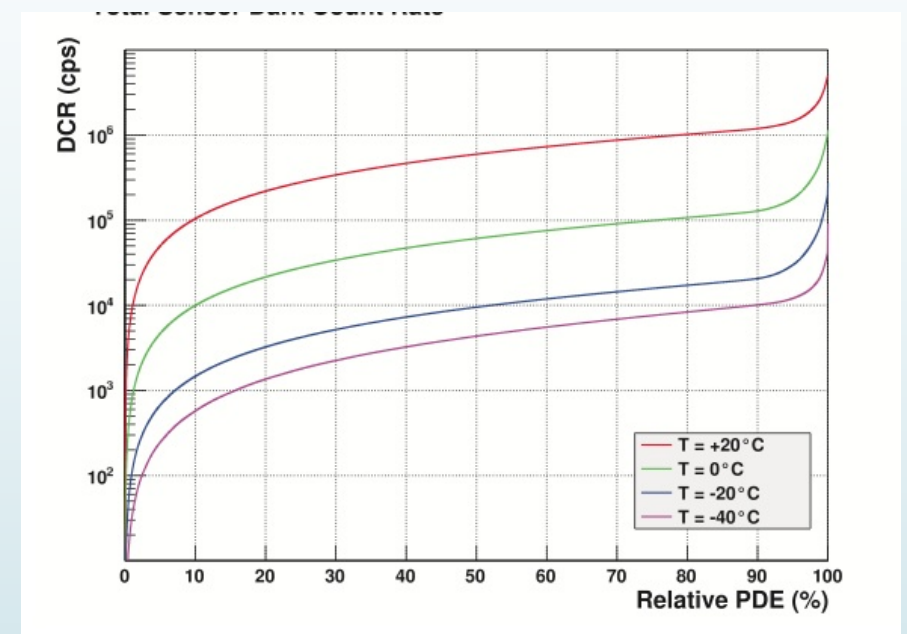
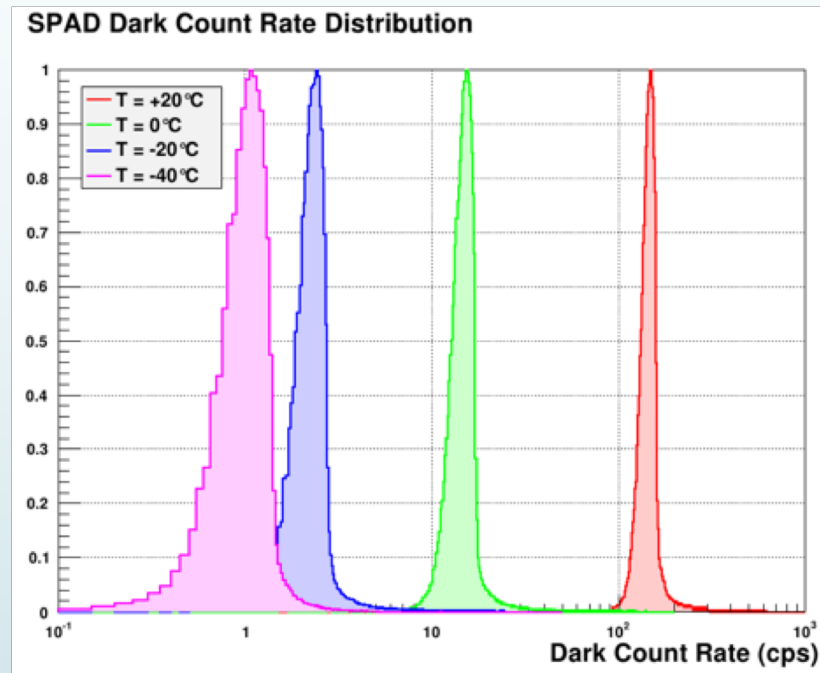


- ❖ 2 x 2 array of sensors
- ❖ 6396 cells/sensor
- ❖ 60 x 40 μm^2 cells
- ❖ chip size 7.8 x 7.2 mm^2
- ❖ **peak PDE ~ 30% @430 nm**
- ❖ modified 0.18 μm 5M CMOS

Exemplary illustrations of the advantages of this design:

1. Spotting hot cells and disabling their output

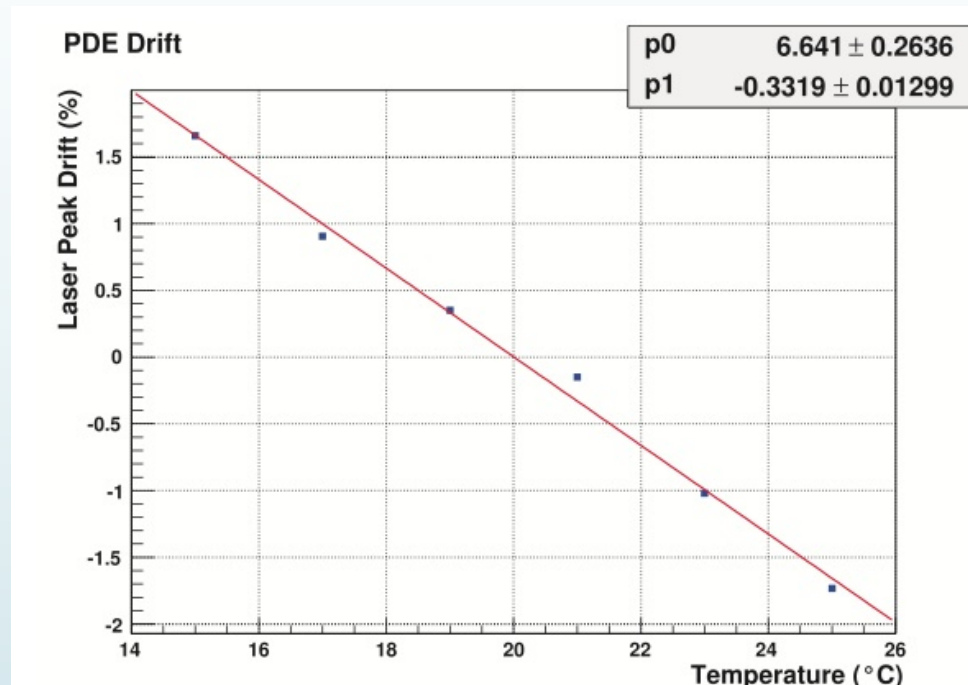
Since individual pixels may be enabled/disabled, the DCR of every cell can be measured, possibly identifying the HOT cells:



Typical dark count rate at 20°C and 3.3V excess voltage: ~150cps / diode

Exemplary illustrations of the advantages of this design:
2. Reduced temperature sensitivity

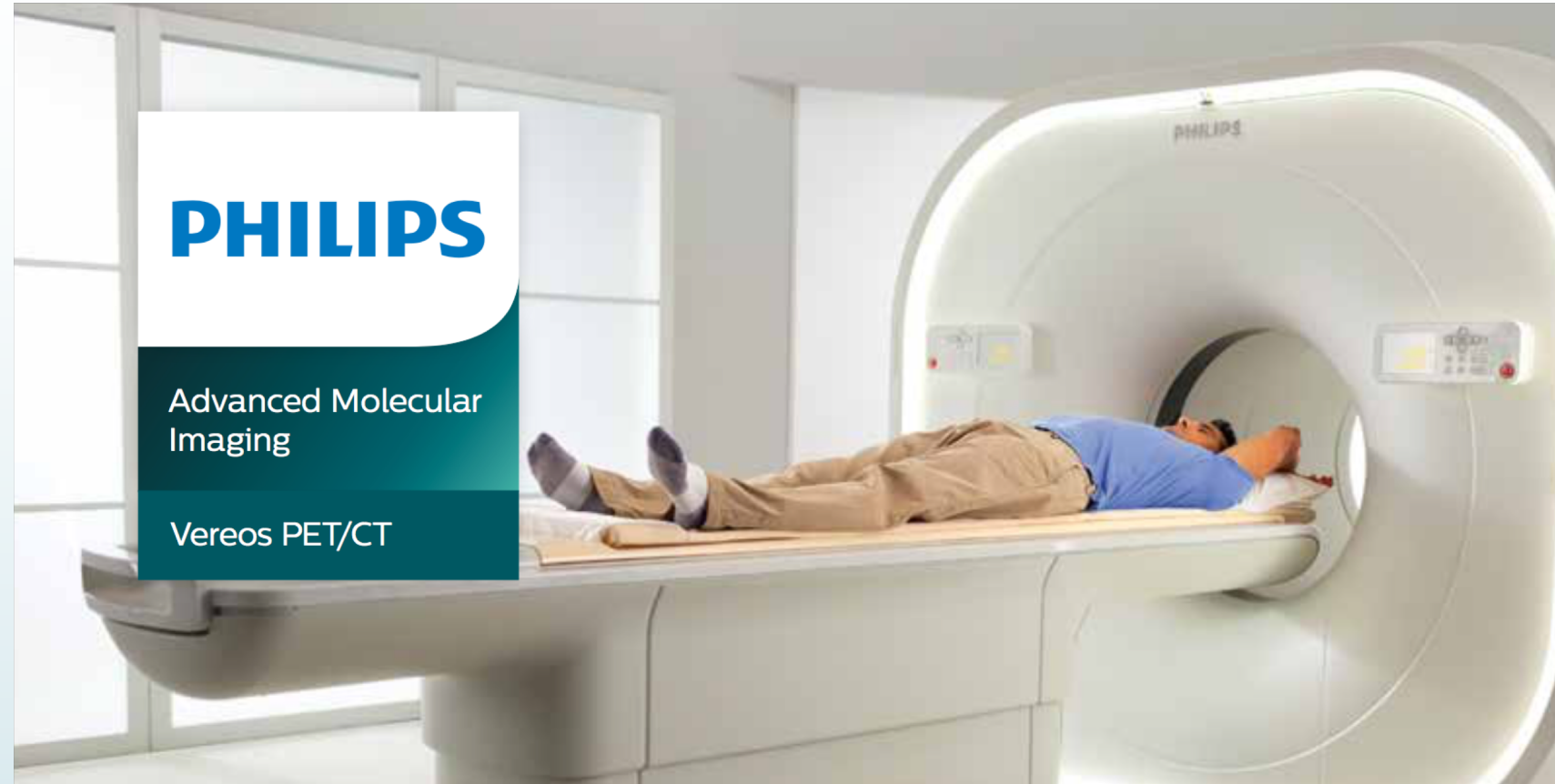
Digital SiPM are insensitive to any change in the breakdown voltage as long as the switching threshold of the gate is reached.



$\approx 0.3\%/C$
Vs
0.5-1%/C in standard SiPM
(operated at +5V)

The remaining drift observed in the digital SiPM is due to the change in the photon detection efficiency, caused by the temperature-dependent avalanche initiation probability.

Is it a successful device?



PHILIPS

Advanced Molecular
Imaging

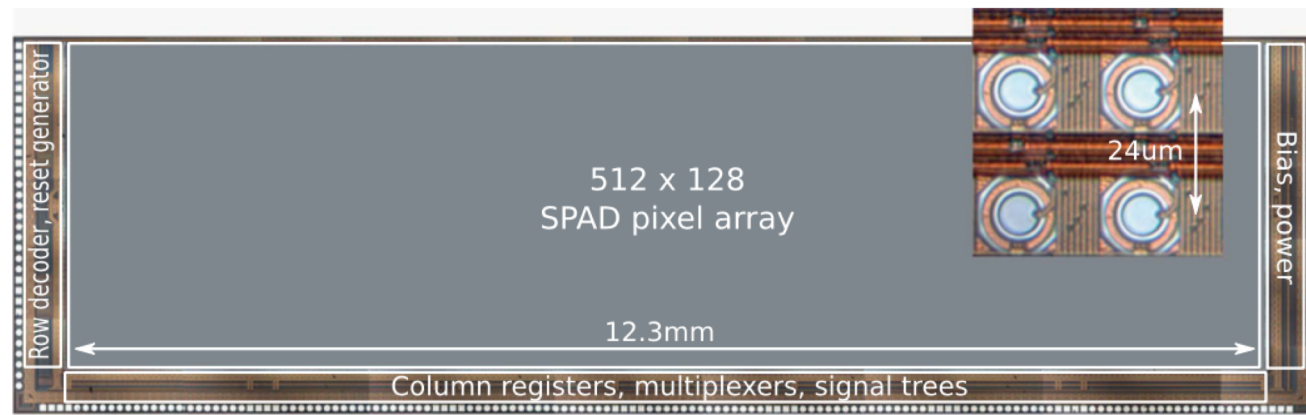
Vereos PET/CT

- 23040 detectors
- 325 ps resolution

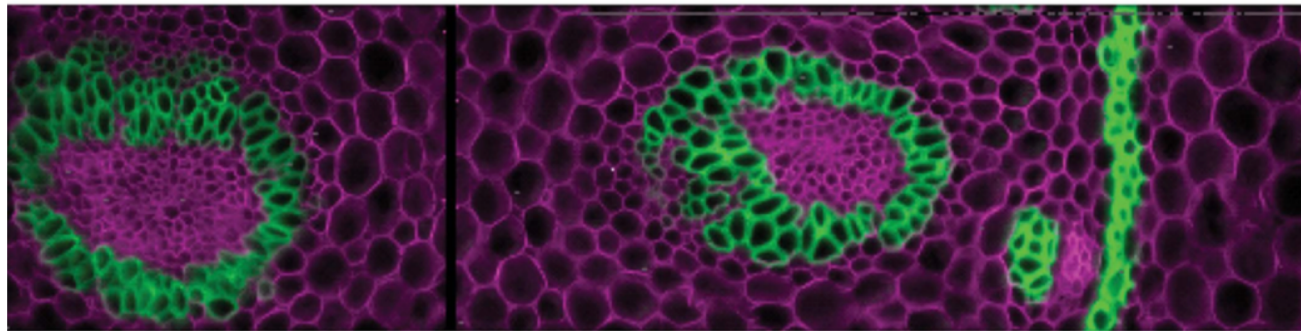
Truly **digital** PET imaging

Philips proprietary Digital Photon Counting technology

The SwissSPAD (Edoardo Charbon et al, SPAD imagers for super resolution localization microscopy enable analysis of fast fluorophore blinking, Nature Scientific Reports | 7:44108 | DOI: 10.1038/srep44108, 2017)



a

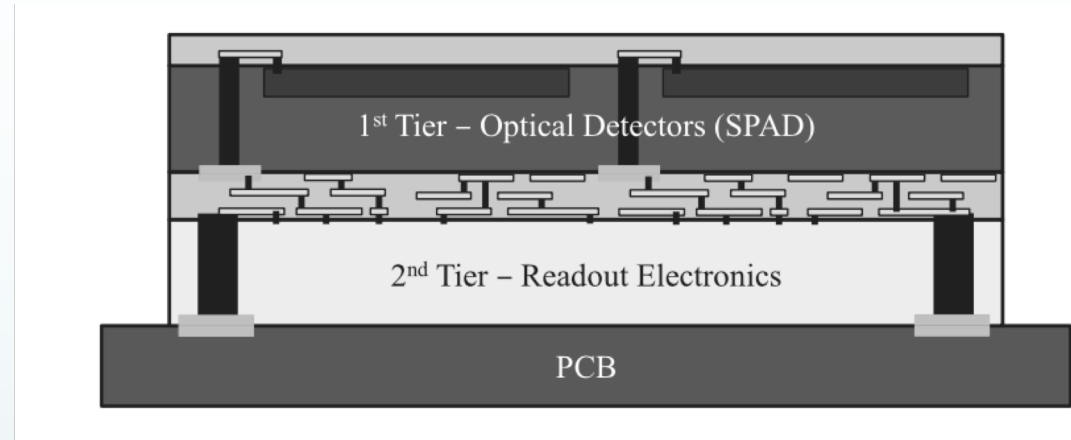


multicolor fuorescence image of a thin slice of a plant root stained with a mixture of fluorescent dyes

- 24 µm pixel pitch
- Rolling shutter readout (6.4 µs frame period)
- Native Fill Factor (FF) 5%
- FF enhancement by micro-lensing: 12
- Achieved super-resolution: 80 nm

The next frontier:

3D vertical integration, to turn a sensor into a SMART sensor, with intelligence on board



Silicon hybrid SPAD with high-NIR-sensitivity for TOF applications

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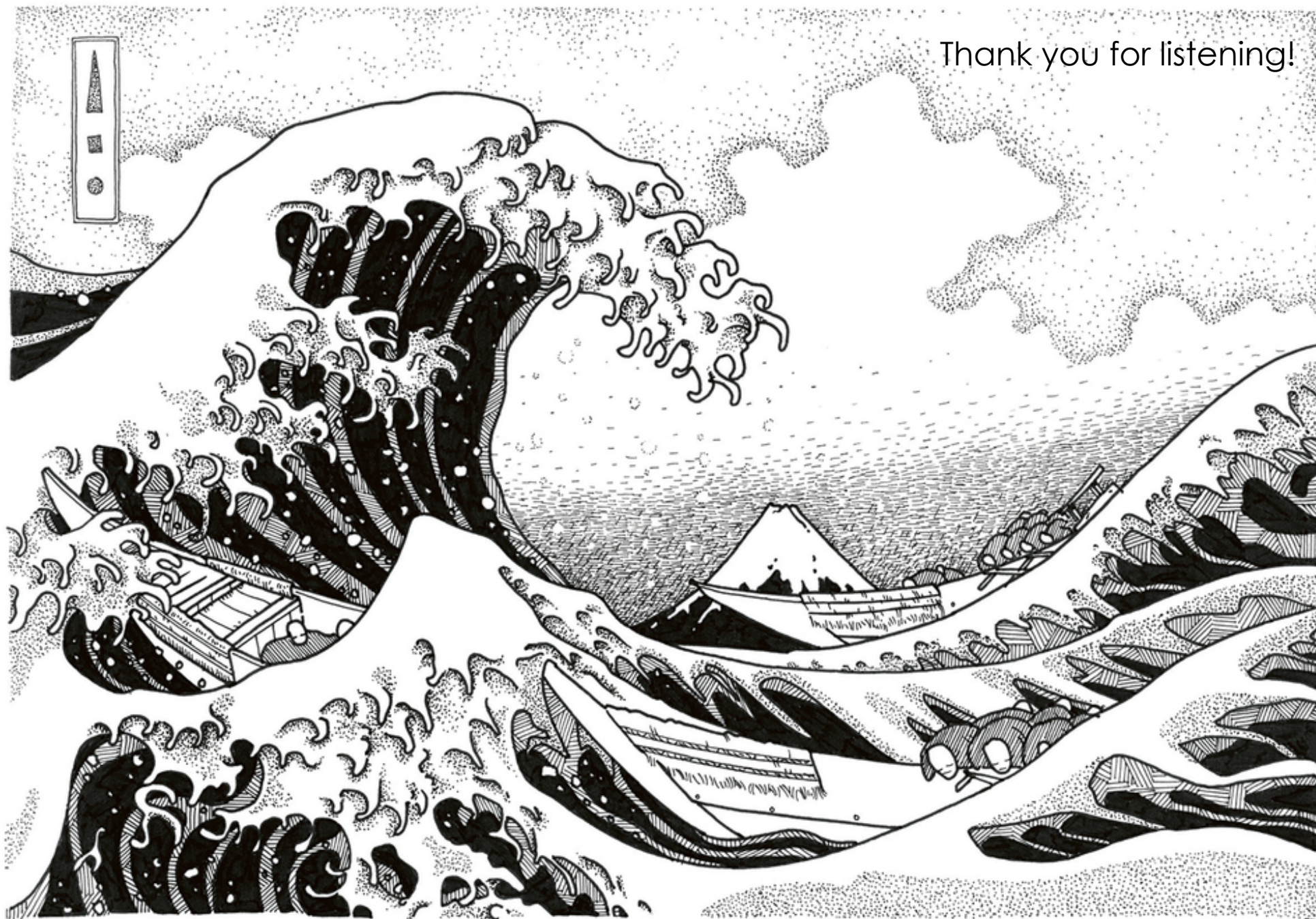
IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 63, NO. 4, AUGUST 2016

A 2D Proof of Principle Towards a 3D Digital SiPM in HV CMOS With Low Output Capacitance

Frédéric Nolet, Vincent-Philippe Rhéaume, Samuel Parent, Serge A. Charlebois, *Member, IEEE*, Réjean Fontaine, *Senior Member, IEEE*, and Jean-François Pratte, *Member, IEEE*

One of the latest
HAMAMATSU developments


Thank you for listening!





Supplementary Slides

High-dimensional intracity quantum cryptography with structured photons

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Ottawa intracity communication link

The OTTAWA experiment

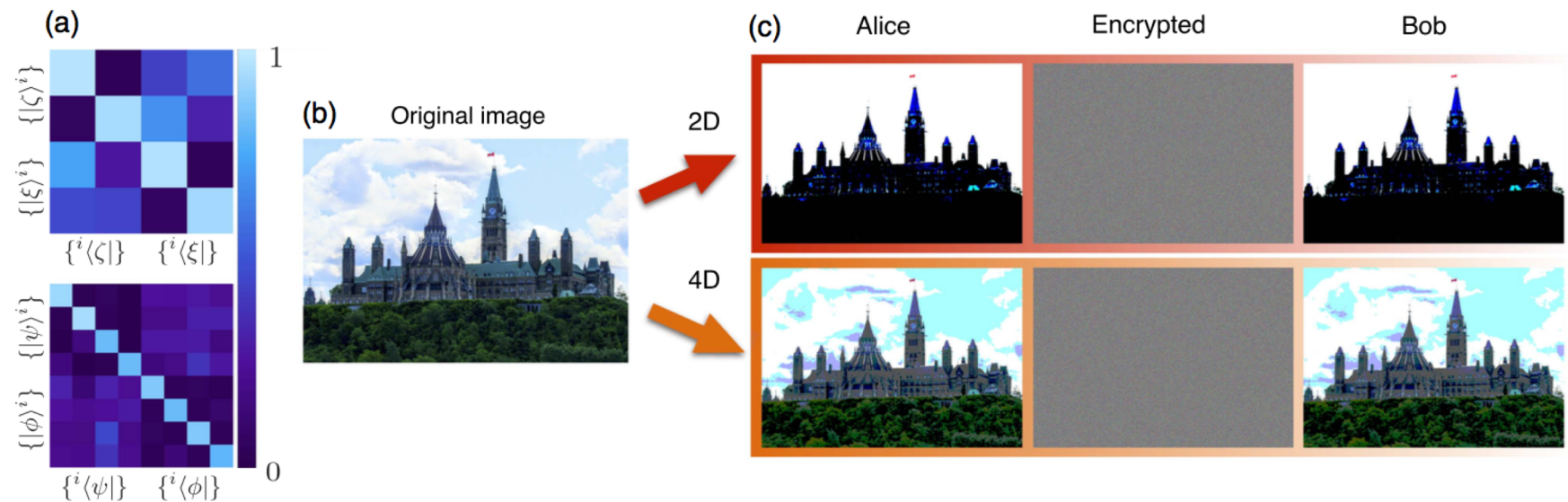
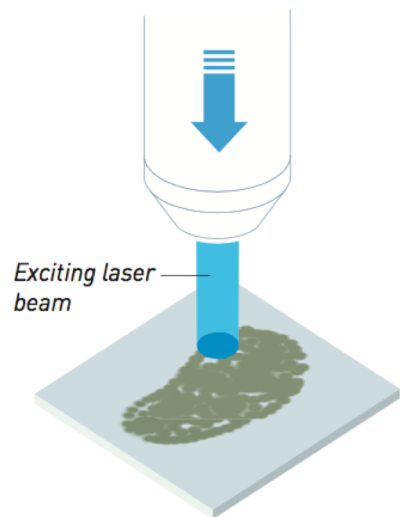


Fig. 3. Simulated encryption of an image with structured photons. (a) Experimentally measured probability-of-detection matrices, $P^{ij} = |{}^i\langle\alpha|\beta\rangle|^2$, where $\alpha, \beta = \{\psi, \phi\}$, for 2D (top row) and 4D (bottom row) structured photons with turbulence. These matrices have the corresponding bit error rates of $Q^{2D} = 5\%$ and $Q^{4D} = 11\%$, respectively. (b) Image of the Parliament of Canada that Alice encrypts and sends to Bob through a classical channel using their shared secret key. (c) Alice discretizes her intended image (left column) with d levels, where d is the encryption dimension, such that each pixel corresponds to three single photons (RGB values, leading to d^3 colors per pixel) that she sends to Bob. Using the experimentally measured probability-of-detection matrices (a), Alice then adds the shared secret key, generated from a BB84 protocol, on top of her discretized image to encrypt it (middle column). Bob decrypts Alice's sent image with his shared key to recover the image (right column). Implementing a 4-dimensional state clearly allows the ability to send more information per photon, where, in the ideal case, Alice can send twice the amount of information with respect to 2-dimensional states. However, due to noise present in the channel, we experimentally obtain an increase of 1.51 in the amount of information sent by Alice with respect to the case of 2-dimensional states. Image credit: Norman Bouchard.

The principle of the Noble prize technique (supplementary material on the Nobel academy web site)

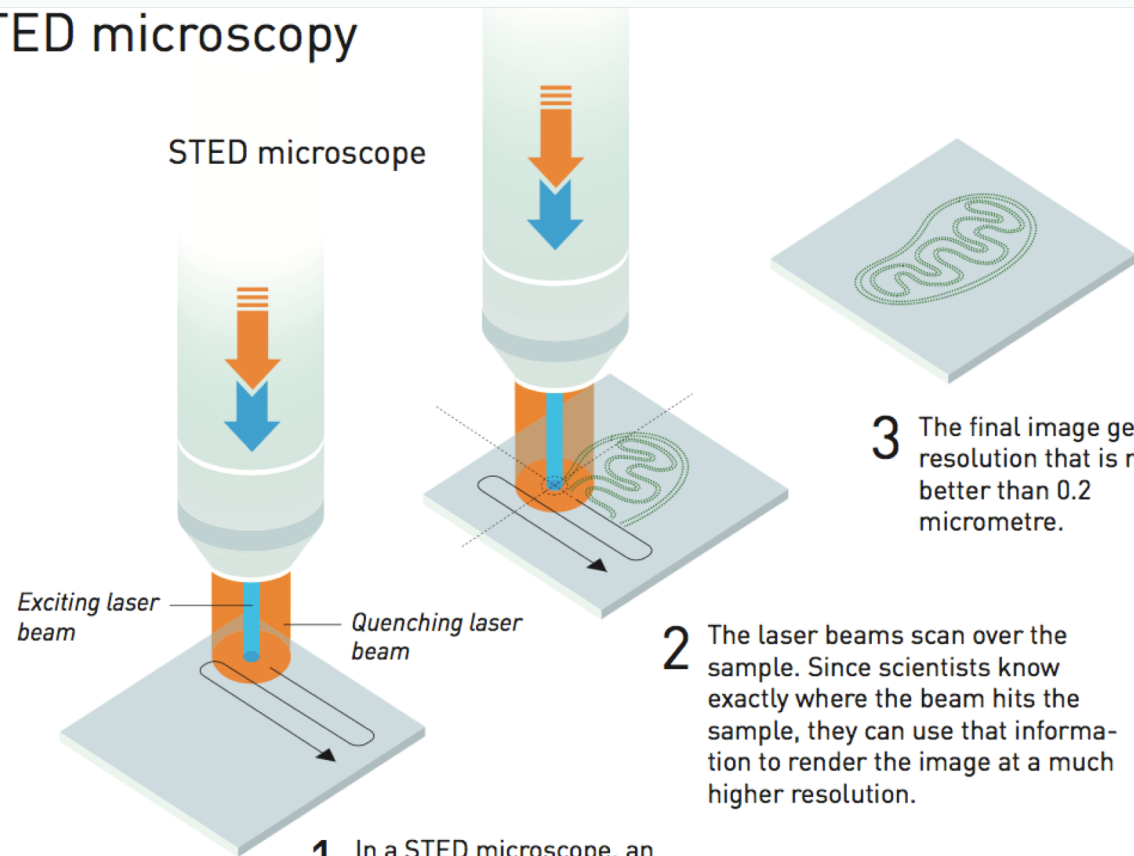
The principle of STED microscopy

Regular optical microscope



In a regular optical microscope, the contours of a mitochondrion can be distinguished, but the resolution can never get better than 0.2 micrometres.

STED microscope

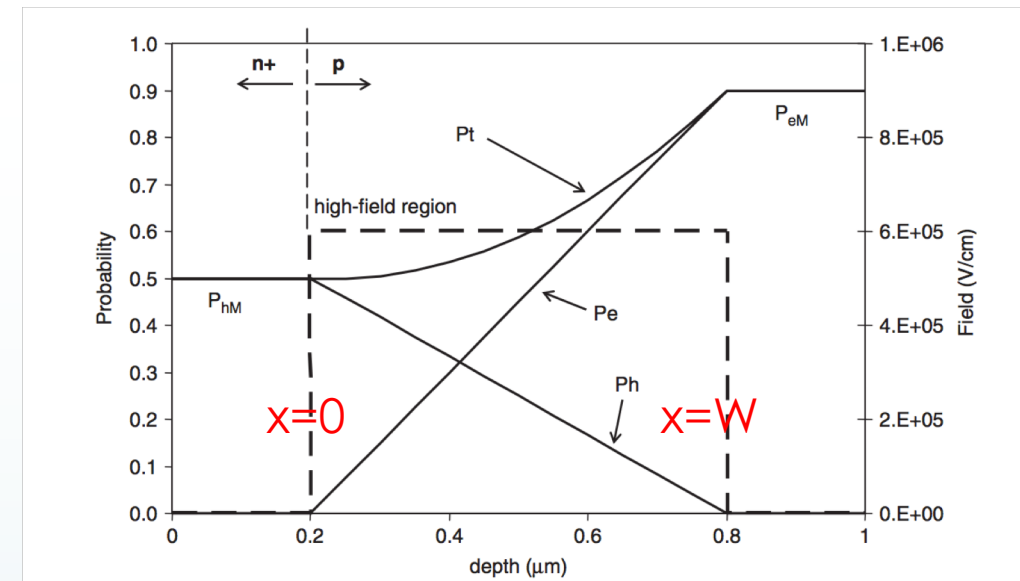


1 In a STED microscope, an annular laser beam quenches all fluorescence except that in a nanometre-sized volume.

2 The laser beams scan over the sample. Since scientists know exactly where the beam hits the sample, they can use that information to render the image at a much higher resolution.

3 The final image gets a resolution that is much better than 0.2 micrometre.

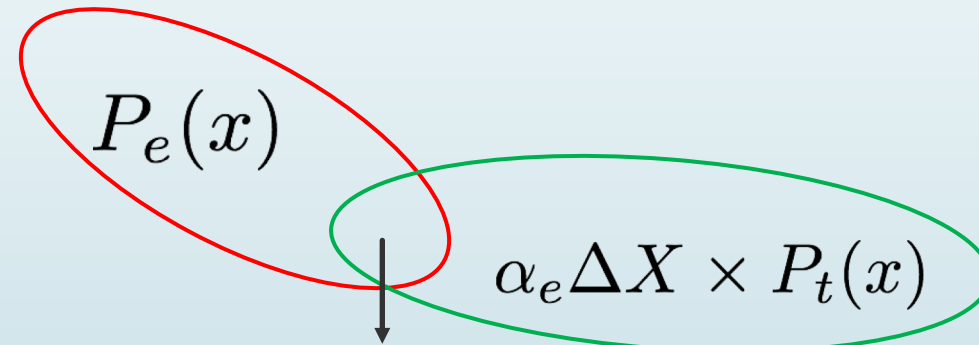
On triggering probability and bias voltage (ref.3)



$$P_t(x) = 1 - (1 - P_e(x)) \times (1 - P_h(x)) = P_e(x) + P_h(x) - P_e(x)P_h(x)$$

How is P_e changing when I move from x to $x+\Delta x$?

1. Probability that the electron triggers an avalanche in x



2. Probability that the electron induces an ionization in ΔX and either the pair triggers an avalanche in x

$$P_e(x) \times \alpha_e \Delta X \times P_t(x) \quad \text{3. Joint probability}$$

Working out the math, you get the equations defining the trends with x of P_e and P_h :

$$\frac{dP_e}{dx} = (1 - P_e)\alpha_e[P_e + P_h - P_eP_h]$$

$$\frac{dP_h}{dx} = -(1 - P_h)\alpha_h[P_e + P_h - P_eP_h]$$

$$P_e(0) = 0$$

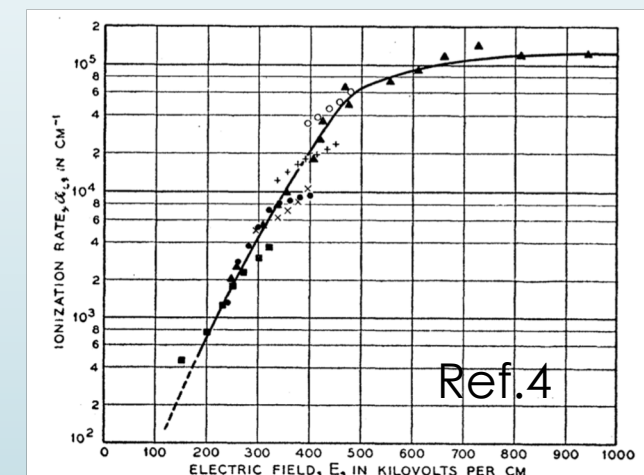
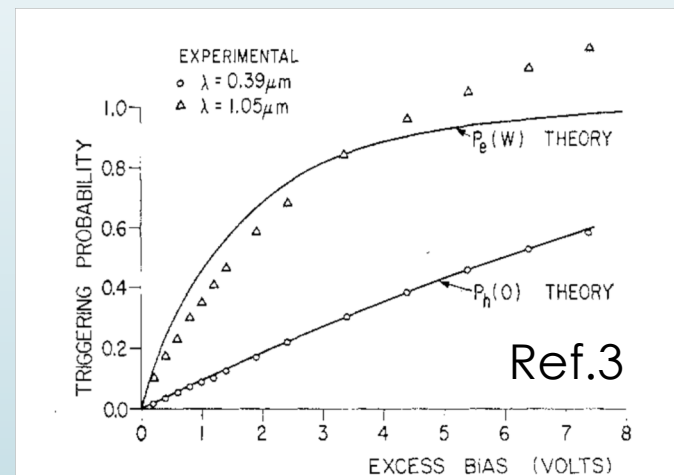
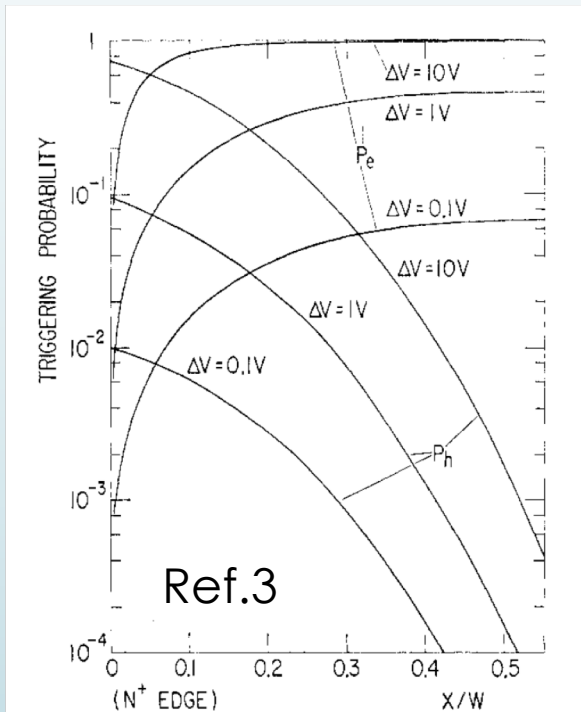
$$P_h(W) = 0.$$

Boundary conditions

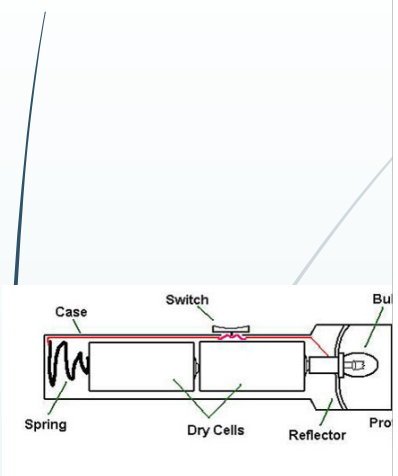
Where α_e, α_h the **IONIZATION COEFFICIENTS**, depend on the electric field (i.e. the bias) as

$$\alpha = a \times e^{\frac{-b}{E}}$$

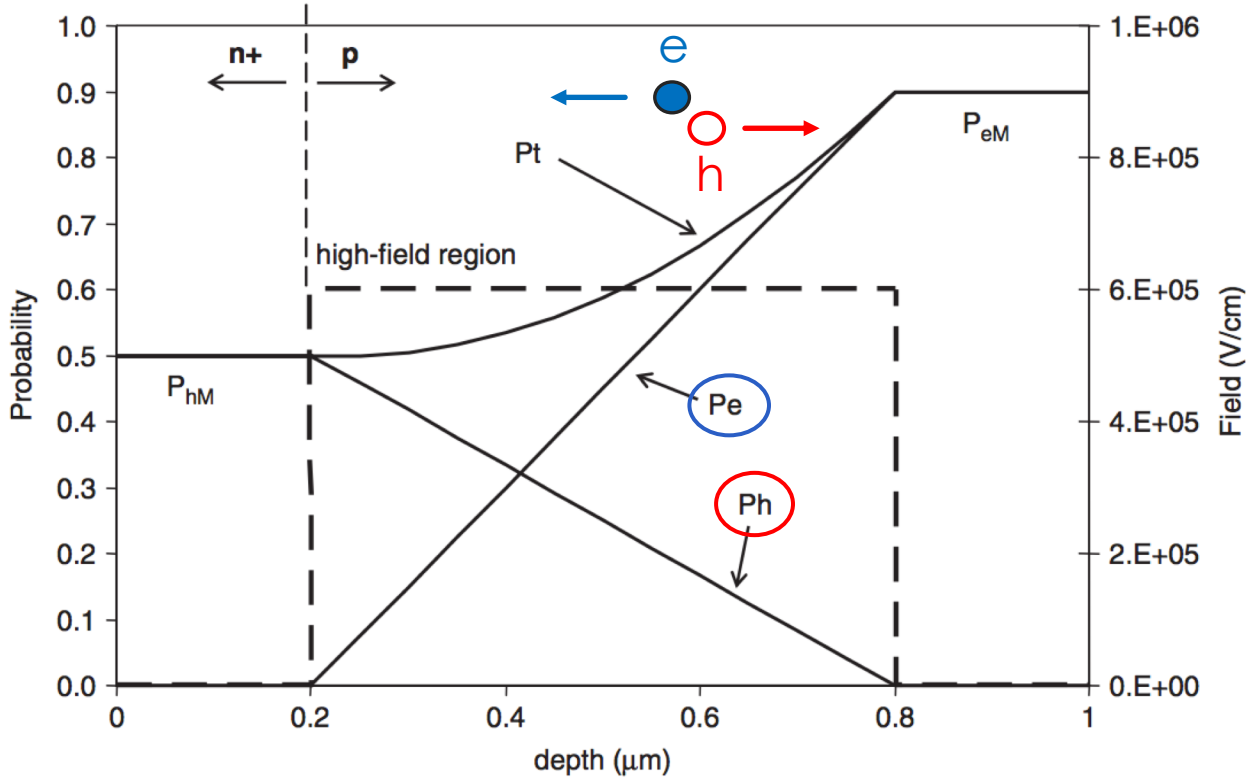
Where $a \approx 10^6$, $b \approx 2 \times 10^6$



Spectral Response: I have to tailor my junction to maximize the probability to trigger an avalanche:

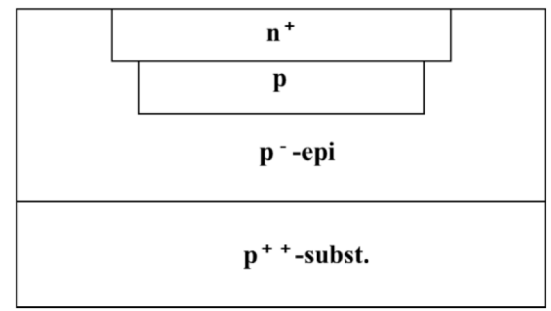


Light in



n-on-p junction:

- ❖ Not ideal for blue
- ❖ Good enough for green
- ❖ Bad for red

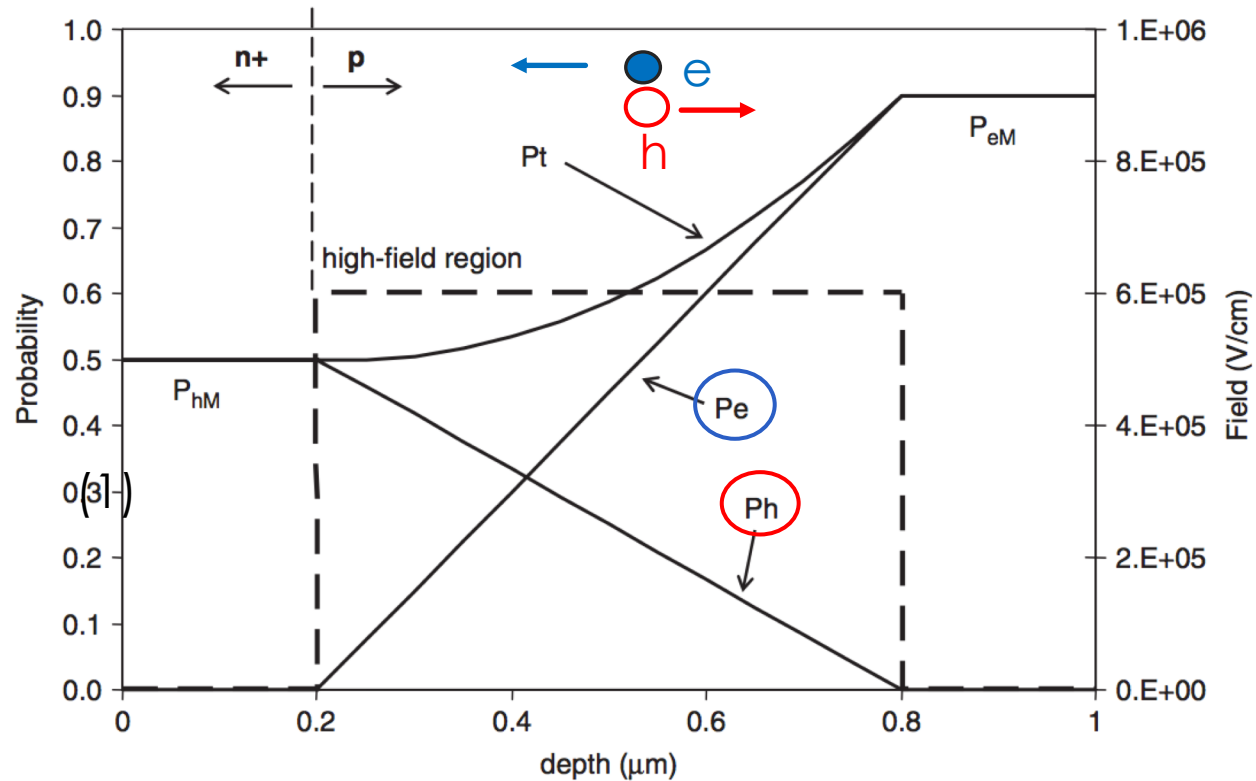


Avalanche triggering probability vs photo-absorption position (ref. 1)

$$P_t = 1 - (1 - P_e) \times (1 - P_h) = P_e + P_h - P_e P_h$$

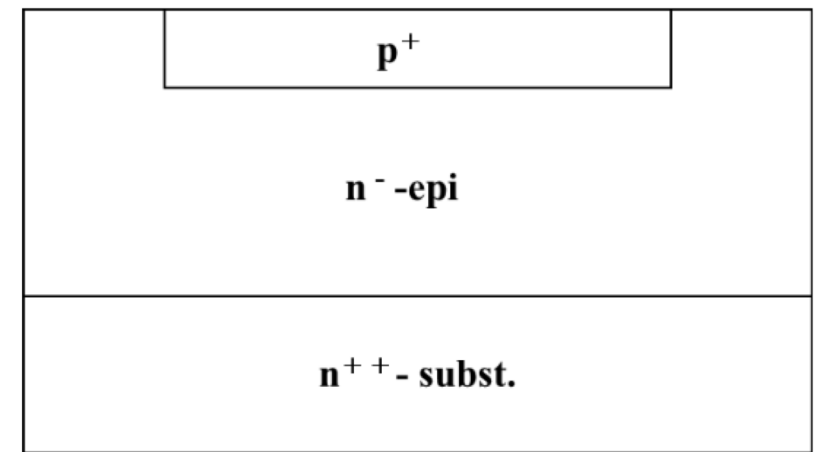
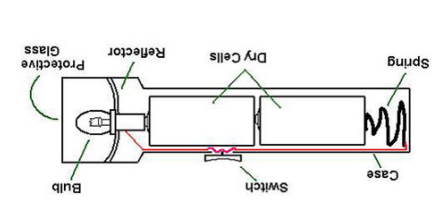
P_t = total triggering probability
 P_e = electron triggering probability
 P_h = hole triggering probability

I have to tailor my junction to maximize the probability to trigger an avalanche:



p-on- junction:

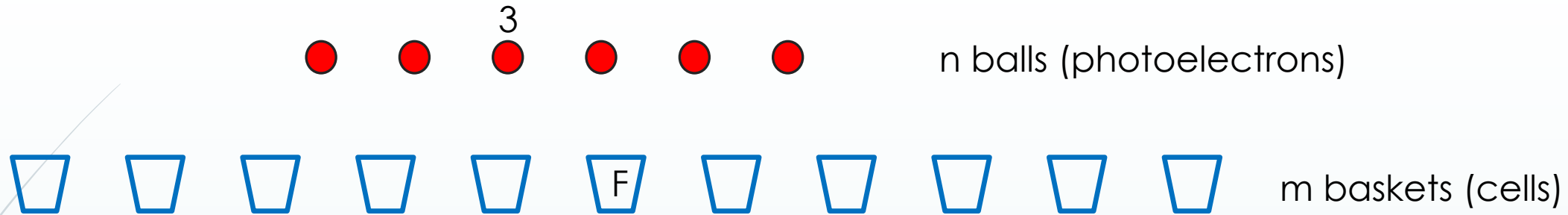
- ❖ Optimized for blue
- ❖ Fair enough for green
- ❖ Worse for red



Holes & electrons were not born equal and the ionization rate of "e" is about double wrt "h"

⇒ if I go to p-on-n and I have a shallow junction, I maximize the triggering probability also for blue light

About balls & baskets [see also Stoykov et al., 2007 JINST 2 P06005]



Presume that the balls are randomly thrown into the baskets. Then:

❖ The probability of a ball (say 3) to get into a specific basket (say F) is $1/m = m^{-1}$

⇒ The probability of **NOT being hit** is $(1 - m^{-1})$

⇒ The probability that **NONE** of the n balls enters F is $(1 - m^{-1})^n$
(assuming the events to be uncorrelated)

⇒ The probability to have **ONE OR MORE** balls in F is $p = (1 - (1 - m^{-1})^n)$

❖ But F is like any other basket ⇒ I can turn the problem in the same category of the “coin toss” statistics (Bernoullian or Binomial), where the coin is not a fair coin but the probability to get “head” is p:

⇒ The mean number of baskets having at least one ball is $\bar{N} = m \times p$

⇒ The standard deviation in the number of cells having at least one ball is $\sigma = \sqrt{m \times p \times (1 - p)}$

As long as the number of baskets (cells) is large,

$$1 - m^{-1} \simeq e^{-\frac{1}{m}}$$
$$p \simeq 1 - e^{-\frac{n}{m}} = 1 - e^{-\frac{N_{photons} \times PDE}{N_{cells}}}$$

And I get the magic formula (together with the fact that the standard deviation in the response, i.e. the fluctuations, do increase since the response is affected by the randomness of the detection process)

About the ENF: formulas can help you in a very effective way to perform a comparison between different solutions/technologies

Referring again to APD, another relevant figure of merit is the **Excess Noise Factor (ENF)**, essentially measuring the fluctuations due to the multiplication process:

$$ENF = \left(\frac{SNR_{in}}{SNR_{out}} \right)^2$$

where $SNR = \frac{Signal}{Noise}$

and $SNR_{in} = \sqrt{N}$ Being N the number of photo-electrons and presuming Poissonian fluctuations

Since*:

$$ENF_{SiPM} = \frac{1 + P_{AP}}{1 + \ln(1 - P_{Xtalk})}$$

- ❖ P_{AP} = After-pulsing probability
- ❖ P_{Xtalk} = Cross-talk probability

*Sergey Vinogradov, Advanced Photon Counting Techniques VI, edited by Mark A. Itzler, Joe C. Campbell, Proc. of SPIE Vol. 8375, 83750S, 2012

Assuming 5% after-pulsing and 10% Optical cross talk, I have $ENF_{SiPM} = 1.17$,
To be compared to these exemplary figures for APD:

Typical values of k, X and F for Si, Ge and InGaAs

Detector Type	Ionization Ratio (k)	X-Factor -	Typical Gain (M)	Excess Noise Factor (at typical gain) (F)
Silicon ("reach-through" structure)	0.02	0.3	150	4.9
Silicon Epitaxial APDs	0.06	0.45	100	7.9
Silicon (SLiK™ low-k structure)	0.002	0.17	500	3.0
Germanium	0.9	0.95	10	9.2
InGaAs	0.45	0.7- 0.75	10	5.5